

US008760007B2

## (12) United States Patent

Joannopoulos et al.

#### (54) WIRELESS ENERGY TRANSFER WITH HIGH-Q TO MORE THAN ONE DEVICE

(75) Inventors: John D. Joannopoulos, Belmont, MA

(US); Aristeidis Karalis, Boston, MA (US); Marin Soljacic, Belmont, MA

(US)

(73) Assignee: Massachusetts Institute of Technology,

Cambridge, MA (US)

(\*) Notice: Subject to any disclaimer, the term of this patent is extended or adjusted under 35

U.S.C. 154(b) by 345 days.

This patent is subject to a terminal dis-

claimer.

(21) Appl. No.: 12/639,963

(22) Filed: Dec. 16, 2009

(65) **Prior Publication Data** 

US 2010/0127575 A1 May 27, 2010

#### Related U.S. Application Data

- (63) Continuation of application No. 12/553,957, filed on Sep. 3, 2009, which is a continuation of application No. 11/481,077, filed on Jul. 5, 2006, now Pat. No. 7,741,734.
- (60) Provisional application No. 60/698,442, filed on Jul. 12, 2005.
- (51) **Int. Cl. H02J 17/00 H01Q 9/04**

(2006.01) (2006.01) (2006.01)

**B60L 11/18** (2006.01) **H02J 5/00** (2006.01)

(52) U.S. Cl.

H02J 5/005 (2013.01)

### (10) Patent No.:

US 8,760,007 B2

(45) **Date of Patent:** 

\*Jun. 24, 2014

#### (58) Field of Classification Search

#### (56) References Cited

#### U.S. PATENT DOCUMENTS

645,576 A 3/1900 Tesla 649,621 A 5/1900 Tesla

(Continued)

#### FOREIGN PATENT DOCUMENTS

CA 142352 8/1912 DE 38 24 972 1/1989

(Continued)

#### OTHER PUBLICATIONS

John C. Schuder, Powering an Artificail Heart: Birth of the Inductively Coupled-Radio Frequency System in 1960, Artificaial Organ, 2002 \*

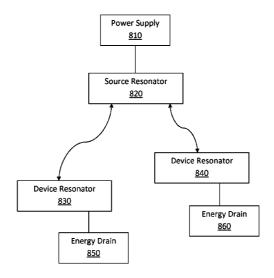
#### (Continued)

Primary Examiner — Fritz M Fleming (74) Attorney, Agent, or Firm — Fish & Richardson P.C.

#### (57) ABSTRACT

Described herein are embodiments of a source high-Q resonator, optionally coupled to an energy source, a second high-Q resonator, optionally coupled to an energy drain that may be located a distance from the source resonator. A third high-Q resonator, optionally coupled to an energy drain that may be located a distance from the source resonator. The source resonator and at least one of the second resonator and third resonator may be coupled to transfer electromagnetic energy from said source resonator to said at least one of the second resonator and third resonator.

#### 44 Claims, 8 Drawing Sheets



# US 8,760,007 B2 Page 2

(56)			Referen	ces Cited	6,609,023			Fischell et al.
		U.S.	PATENT	DOCUMENTS	6,631,072 6,650,227	В1	11/2003	
	797 412		4/1905	T1-	6,664,770 6,673,250		1/2003	Kuennen et al.
	787,412 1,119,732		12/1914		6,683,256	B2	1/2004	Kao
	2,133,494	A	10/1938		6,696,647			Ono et al.
	3,517,350		6/1970		6,703,921 6,731,071			Wuidart et al. Baarman
	3,535,543 3,780,425		10/1970 12/1973		6,749,119			Scheible et al.
	3,871,176			Schukei	6,772,011		8/2004	
	4,088,999			Fletcher et al.	6,798,716 6,803,744		9/2004 10/2004	Charych
	4,095,998 4,180,795			Hanson Matsuda et al 340/448	6,806,649			Mollema et al.
	4,280,129		7/1981		6,812,645	B2	11/2004	Baarman
	4,450,431	A *		Hochstein 340/447	6,825,620			Kuennen et al.
	4,588,978		5/1986		6,831,417 6,839,035			Baarman Addonisio et al.
	5,027,709 5,033,295		7/1991 7/1991	Schmid et al.	6,844,702	B2		Giannopoulos et al.
	5,034,658			Hierig et al.	6,856,291			Mickle et al.
	5,053,774			Schuermann et al.	6,858,970 6,906,495			Malkin et al. Cheng et al.
	5,070,293 5,118,997			Ishii et al. El-Hamamsy	6,917,163			Baarman
	5,216,402			Carosa	6,917,431	B2		Soljacic et al.
	5,229,652	A	7/1993	Hough	6,937,130			Scheible et al.
	5,287,112			Schuermann	6,960,968 6,961,619		11/2005	Odendaal et al. Casev
	5,341,083 5,367,242			Klontz et al. Hulman	6,967,462		11/2005	
				Schuermann	6,975,198			Baarman
	5,408,209			Tanzer et al.	6,988,026 7,027,311			Breed et al. Vanderelli et al.
	5,437,057 5,455,467	A 4 *	7/1995	Richley et al. Young et al 307/104	7,035,076			Stevenson
	5,493,691			Barrett	7,042,196	B2	5/2006	Ka-Lai et al.
	5,522,856	A	6/1996	Reineman	7,069,064			Govorgian et al.
	5,528,113			Boys et al.	7,084,605 7,116,200			Mickle et al. Baarman et al.
	5,541,604 5,550,452		7/1996 8/1996	Shirai et al.	7,118,240			Baarman et al.
	5,565,763			Arrendale et al.	7,126,450			Baarman et al.
	5,630,835			Brownlee	7,127,293 7,132,918			MacDonald Baarman et al.
	5,697,956 5,703,461		12/1997	Bornzin Minoshima et al.	7,147,604			Allen et al.
	5,703,573	A *	12/1997	Fujimoto et al 340/10.3	7,180,248	B2		Kuennen et al.
	5,710,413	A	1/1998	King et al.	7,191,007			Desai et al.
	5,742,471			Barbee, Jr. et al. Schwind	7,193,418 7,212,414			Freytag Baarman
	5,821,728 5,821,731			Kuki et al.	7,233,137			Nakamura et al.
	5,864,323	A	1/1999	Berthon	7,239,110		7/2007	Cheng et al.
	5,898,579			Boys et al.	7,248,017 7,251,527		7/2007	Cheng et al.
	5,903,134 5,923,544		3/1999 7/1999	Takeuchi Urano	7,288,918			DiStefano
	5,940,509			Jovanovich et al.	7,375,492			Calhoon et al.
	5,957,956			Kroll et al.	7,375,493 7,378,817			Calhoon et al. Calhoon et al.
	5,959,245 5,986,895			Moe et al. Stewart et al.	7,382,636			Baarman et al.
	5,993,996		11/1999		7,385,357	B2		Kuennen et al.
	5,999,308			Nelson et al.	7,443,135 7,462,951		10/2008	Cho Baarman
	6,012,659 6,047,214			Nakazawa et al. Mueller et al.	7,466,213			Lobl et al.
	6,066,163		5/2000		7,474,058	B2	1/2009	Baarman
	6,067,473	A	5/2000	Greeninger et al.	7,492,247			Schmidt et al.
	6,108,579			Snell et al.	7,514,818 7,518,267			Abe et al. Baarman
	6,127,799 6,176,433			Krishnan Uesaka et al.	7,525,283			Cheng et al.
	6,184,651			Fernandez et al.	7,545,337			Guenther
	6,207,887			Bass et al.	7,599,743 7,615,936			Hassler, Jr. et al. Baarman et al.
	6,232,841 6,238,387			Bartlett et al. Miller, III	7,639,514			Baarman
	6,252,762			Amatucci	7,741,734	B2 *	6/2010	Joannopoulos et al 307/104
	6,436,299	B1		Baarman et al.	7,795,708		9/2010	
	6,450,946			Forsell Proven et al.	7,825,543 7,843,288			Karalis et al. Lee et al.
	6,452,465 6,459,218			Brown et al. Boys et al.	7,863,859		1/2010	
	6,473,028	B1	10/2002	Luc	8,022,576	B2	9/2011	Joannopoulos et al.
	6,483,202		11/2002		8,076,800			Joannopoulos et al.
	6,515,878			Meins et al.	8,076,801			Karalis et al.
	6,535,133 6,561,975			Gohara Pool et al.	8,084,889 8,097,983			Joannopoulos et al. Karalis et al.
	6,563,425			Nicholson et al.	8,131,378		3/2012	Greenberg et al.
	6,597,076			Scheible et al.	8,178,995		5/2012	Amano et al.

## US 8,760,007 B2

Page 3

(56)	Referen	nces Cited	2006/0181242			Freed et al.
IIS	PATENT	DOCUMENTS	2006/0184209 2006/0184210			John et al. Singhal et al.
0.5.	LATINI	DOCOMENTS	2006/0185809			Elfrink et al.
8,362,651 B2	1/2013	Hamam et al.	2006/0199620			Greene et al.
8,395,282 B2	3/2013	Joannopoulos et al.	2006/0202665 2006/0205381		9/2006 9/2006	Hsu Beart et al.
8,395,283 B2 8,400,018 B2	3/2013 3/2013	Joannopoulos et al. Joannopoulos et al.	2006/0214626			Nilson et al.
8,400,019 B2	3/2013		2006/0219448			Grieve et al.
8,400,020 B2		Joannopoulos et al.	2006/0238365 2006/0270440			Vecchione et al. Shearer et al.
8,400,021 B2 8,400,022 B2		Joannopoulos et al. Joannopoulos et al.	2006/02/0440			Shearer et al.
8,400,022 B2 8,400,023 B2	3/2013	Joannopoulos et al.	2007/0010295	A1	1/2007	Greene et al.
8,400,024 B2		Joannopoulos et al.	2007/0013483			Stewart
2002/0032471 A1		Loftin et al.	2007/0016089 2007/0021140			Fischell et al. Keyes, IV et al.
2002/0105343 A1 2002/0118004 A1		Scheible et al. Scheible et al.	2007/0024246			Flaugher
2002/0130642 A1	9/2002	Ettes et al.	2007/0064406		3/2007	
2002/0167294 A1		Odaohhara	2007/0069687 2007/0096875		3/2007 5/2007	Waterhouse et al.
2003/0038641 A1 2003/0062794 A1		Scheible Scheible et al.	2007/0090879			Kohl et al.
2003/0062980 A1		Scheible et al.	2007/0117596			Greene et al.
2003/0071034 A1		Thompson et al.	2007/0126650			Guenther Lee et al.
2003/0124050 A1 2003/0126948 A1	7/2003	Yadav et al. Yadav et al.	2007/0145830 2007/0171681			Baarman
2003/0120948 A1 2003/0160590 A1		Schaefer et al.	2007/0176840			Pristas et al.
2003/0199778 A1		Mickle et al.	2007/0178945			Cook et al.
2003/0214255 A1		Baarman et al.	2007/0182367 2007/0208263		8/2007 9/2007	Partovi John et al.
2004/0000974 A1 2004/0026998 A1		Odenaal et al. Henriott et al.	2007/0222542		9/2007	Joannopoulos et al.
2004/0100338 A1	5/2004		2007/0267918		11/2007	
2004/0113847 A1		Qi et al.	2007/0276538 2008/0012569		11/2007	Kjellsson et al. Hall et al.
2004/0130425 A1 2004/0130915 A1		Dayan et al. Baarman	2008/0012309			Cook et al.
2004/0130915 A1 2004/0130916 A1		Baarman	2008/0030415			Homan et al.
2004/0142733 A1	7/2004		2008/0067874		3/2008	Tseng
2004/0150934 A1		Baarman Bulai et al	2008/0191638 2008/0197710			Kuennen et al. Kreitz et al.
2004/0189246 A1 2004/0201361 A1		Bulai et al. Koh et al.	2008/0211320			Cook et al.
2004/0222751 A1		Mollema et al.	2008/0265684		10/2008	
2004/0227057 A1	11/2004		2008/0266748 2008/0278264		10/2008	Lee Karalis et al.
2004/0232845 A1 2004/0233043 A1	11/2004	Baarman Yazawa et al.	2009/0010028			Baarman et al.
2004/0267501 A1		Freed et al.	2009/0015075			Cook et al.
2005/0007067 A1		Baarman et al.	2009/0033564 2009/0045772			Cook et al. Cook et al.
2005/0021134 A1 2005/0027192 A1	1/2005	Opie Govari et al.	2009/0043772			Cook et al.
2005/0027132 A1 2005/0033382 A1	2/2005		2009/0058189			Cook et al.
2005/0085873 A1		Gord et al.	2009/0067198 2009/0072627		3/2009	Graham et al. Cook et al.
2005/0093475 A1 2005/0104064 A1	5/2005 5/2005	Kuennen et al. Hegarty et al.	2009/0072628			Cook et al.
2005/0104004 A1 2005/0104453 A1	5/2005	Vanderelli et al.	2009/0072629	A1	3/2009	Cook et al.
2005/0116650 A1		Baarman	2009/0079268 2009/0085408		3/2009 4/2009	Cook et al.
2005/0116683 A1 2005/0122058 A1		Cheng et al. Baarman et al.	2009/0085706			Baarman et al.
2005/0122059 A1		Baarman et al.	2009/0096413	A1	4/2009	Patovi et al.
2005/0125093 A1		Kikuchi et al.	2009/0102292			Cook et al.
2005/0127849 A1 2005/0127850 A1		Baarman et al. Baarman et al.	2009/0108679 2009/0108997			Porwal Patterson et al.
2005/0127866 A1		Hamilton et al.	2009/0127937			Widmer et al.
2005/0135122 A1	6/2005	Cheng et al.	2009/0134712			Cook et al.
2005/0140482 A1		Cheng et al.	2009/0146892 2009/0153273		6/2009	Shimizu et al.
2005/0151511 A1* 2005/0156560 A1	7/2005	Chary 320/127 Shimaoka et al.	2009/0160261		6/2009	Elo
2005/0189945 A1		Reiderman	2009/0167449			Cook et al.
2005/0194926 A1		Di Stefano	2009/0174263 2009/0179502			Baarman et al. Cook et al.
2005/0253152 A1 2005/0288739 A1		Klimov et al. Hassler, Jr. et al.	2009/0179302			Kawasaki
2005/0288740 A1		Hassler, Jr. et al.	2009/0195332		8/2009	Joannopoulos et al.
2005/0288741 A1*		Hassler et al 607/61	2009/0195333		8/2009	Joannopoulos et al.
2005/0288742 A1 2006/0001509 A1	1/2005	Giordano et al.	2009/0212636 2009/0213028			Cook et al. Cook et al.
2006/0001309 A1 2006/0022636 A1		Xian et al.	2009/0213028			Cook et al.
2006/0053296 A1	3/2006	Busboom et al.	2009/0224609	A1	9/2009	Cook et al.
2006/0061323 A1		Cheng et al.	2009/0224856			Karalis et al.
2006/0066443 A1 2006/0090956 A1	3/2006 5/2006	Hall Peshkovskiy et al.	2009/0230777 2009/0237194		9/2009 9/2009	Baarman et al. Waffenschmidt et al.
2006/0030930 A1 2006/0132045 A1		Baarman	2009/0237194		10/2009	
2006/0164866 A1		Vanderelli et al.	2009/0243397	A1	10/2009	Cook et al.

(56)	References Cited				FOREIGN PATENT DOCUMENTS				
U.S	3. PATENT	DOCUMENTS		DE	100 29147	12/2001			
				DE	200 16 655	2/2002	H02J 17/00		
2009/0251008 A1	10/2009	Sugaya		DE	102 21 484	11/2003	G06F 1/26		
2009/0267558 A1	10/2009			DE DE	103 04584 10 2005 03629	8/2004 2/2007			
2009/0267709 A1 2009/0267710 A1	10/2009 10/2009	Joannopoulos et al. Joannopoulos et al.		DE	102006044057	4/2008			
2009/0271047 A1	10/2009	Wakamatsu		EP	1335477	8/2003			
2009/0271048 A1		Wakamatsu		EP	1 521 206	4/2005			
2009/0273242 A1				EP	1 524 010	4/2005	A61N 1/372		
2009/0281678 A1	11/2009	Wakamatsu		JP	02-097005	4/1990	H01F 21/06		
2009/0284082 A1	11/2009			JP	4-265875	9/1992	G01R 33/035		
2009/0284083 A1	11/2009			JP JP	6-341410 9-182323	12/1994 7/1997	F15B 15/18 H02J 17/00		
2009/0284218 A1 2009/0284220 A1	11/2009	Mohammadian et al. Toncich et al.		JР	9-182323	11/1997	H02J 7/10		
2009/0284220 A1 2009/0284227 A1	11/2009			JР	10-164837	6/1998	H02M 3/28		
2009/0284245 A1	11/2009			JР	11-75329	3/1999	H02J 17/00		
2009/0284369 A1	11/2009	Toncich et al.		JР	11-188113	7/1999	A61N 1/378		
2009/0286470 A1	11/2009	Mohammadian et al.		JP	2001-309580	11/2001	H02J 17/00		
2009/0286475 A1	11/2009	Toncich et al.		JР	2002-10535	1/2002	H02J 17/00		
2009/0286476 A1	11/2009	Toncich et al.		JP JP	2003-179526	6/2003	H04B 5/02		
2009/0289595 A1	11/2009	Chen et al. Cook et al.		JР	2004-166459 2004-201458	6/2004 7/2004	H02J 7/00 H02M 3/28		
2009/0299918 A1 2010/0038970 A1		Cook et al.		JР	2005-57444	3/2005	H01Q 7/09		
2010/0096934 A1		Joannopoulos et al.		ĴР	2005-149238	6/2005	G06K 19/00		
2010/0102639 A1		Joannopoulos et al.		JР	2006-074848	3/2006	H02J 17/00		
2010/0102640 A1		Joannopoulos et al.		Љ	2007-505480	3/2007	H01F 38/14		
2010/0102641 A1	4/2010			JP	2007-537637	12/2007	H01Q 7/08		
2010/0117455 A1		Joannopoulos et al.		KR	10-2007-0017804	2/2007	H02J 17/00		
2010/0117456 A1		Karalis et al.		SG WO	112842 WO 92/17929	7/2005 10/1992			
2010/0123353 A1 2010/0123354 A1	5/2010	Joannopoulos et al. Joannopoulos et al.		WO	WO 92/17929 WO 93/23908	11/1993			
2010/0123355 A1		Joannopoulos et al.		WO	WO 94/28560	12/1994			
2010/0127573 A1		Joannopoulos et al.		WO	WO 95/11545	4/1995	H02J 17/00		
2010/0127574 A1		Joannopoulos et al.		WO	WO 96/02970	2/1996			
2010/0133918 A1	6/2010	Joannopoulos et al.		WO	WO 98/50993	11/1998			
2010/0133919 A1		Joannopoulos et al.		WO	WO 00/77910	12/2000	H02J 5/00		
2010/0133920 A1		Joannopoulos et al.		WO WO	WO 00/79910 WO 03/092329	12/2000 11/2003			
2010/0148589 A1 2010/0171370 A1		Hamam et al. Karalis et al.		wo	WO 03/096361	11/2003			
2010/0171370 A1 2010/0181844 A1		Karalis et al.		WO	WO 03/096512	11/2003			
2010/0187911 A1		Joannopoulos et al.		WO	WO 2004015885				
2010/0201205 A1		Karalis et al.		WO	WO 2004/038888	5/2004			
2010/0207458 A1		Joannopoulos et al.		WO	WO 2004/055654	7/2004			
2010/0225175 A1		Karalis et al.		WO	WO 2004/073150	8/2004			
2010/0231053 A1 2010/0231163 A1		Karalis et al. Mashinsky		WO WO	WO 2004/073166 WO 2004/073176	8/2004 8/2004			
2010/0231103 A1 2010/0237706 A1		Karalis et al.		WO	WO 2004/073170 WO 2004/073177	8/2004			
2010/0237707 A1		Karalis et al.		WO	WO 2004/112216	12/2004			
2010/0237708 A1		Karalis et al.		WO	WO 2005/024865	3/2005			
2010/0253152 A1		Karalis et al.		WO	WO 2005/060068	6/2005			
2010/0264745 A1		Karalis et al.		WO	WO 2005/109597	11/2005			
2010/0277005 A1	11/2010	Karalis et al.		WO WO	WO 2005/109598 2006/011769	11/2005 2/2006	H04B 7/14		
2010/0289449 A1 2010/0327660 A1		Karalis et al.		WO	WO 2007/008646	1/2007	1104D //14		
2010/0327661 A1		Karalis et al.		WO	WO 2007/020583	2/2007			
2011/0012431 A1		Karalis et al.		WO	WO 2007/042952	4/2007	A61B 5/117		
2011/0018361 A1		Karalis et al.		WO	WO 2007/084716	7/2007			
2011/0025131 A1	2/2011	Karalis et al.		WO	WO 2007/084717	7/2007			
2011/0043046 A1	2/2011	Joannopoulos et al.		WO	WO 2008/109489	9/2008			
2011/0049996 A1		Karalis et al.		WO WO	WO 2008/118178 WO 2009/009559	10/2008 1/2009			
2011/0049998 A1		Karalis et al.		wo	WO 2009/018568	2/2009			
2011/0074218 A1		Karalis et al.		WO	WO 2009/023155	2/2009			
2011/0074347 A1		Karalis et al.		WO	WO 2009/023646	2/2009			
2011/0089895 A1		Karalis et al.		WO	WO 2009/033043	3/2009			
2011/0140544 A1		Karalis et al. Karalis et al.		WO	WO 2009/070730	6/2009			
2011/0148219 A1 2011/0162895 A1		Karalis et al. Karalis et al.		WO	WO 2009/126963	10/2009			
2011/0102893 A1 2011/0169339 A1		Karalis et al.		WO WO	WO 2009/140506 WO 2009/149464	11/2009 12/2009			
2011/0109339 A1 2011/0181122 A1		Karalis et al.		WO	WO 2009/149404 WO 2009/155000	12/2009			
2011/0193419 A1		Karalis et al.		wo	WO 2010/039967	4/2010			
2011/0198939 A1		Karalis et al.		WO	2011/062827	5/2011	G06F 1/26		
2011/0221278 A1		Karalis et al.							
2011/0227528 A1		Karalis et al.			OTHER	PUBLICATIO	NS		
2011/0227530 A1		Karalis et al.		"C :	1 m · · · · =	0 ***	D 01 - 2		
2011/0241618 A1		Karalis et al.		-			ow-Power Short Range		
2012/0068549 A1	5/2012	Karalis et al.		Kadio l	Lnks", Yates et al., 10	5/-/122/04, copy	right 2004 IEEE, IEEE		

#### (56) References Cited

#### OTHER PUBLICATIONS

Transactions on Circuits and Systems—I: Regular Papers, vol. 51, No. 7, Jul. 2004.\*

John C. Schuder et al., "An Inductively Coupled RF System for the Transmission of 1 kW of Power Through the Skin", *IEEE Transactions on Bio-Medical Engineering*, vol. BME-18, No. 4 (Jul. 1971). J. C. Schuder et al., "Energy Transport Into the Closed Chest From a Set of Very-Large Mutually Orthogonal Coils", *Communication Electronics*, vol. 64, pp. 527-534 (Jan. 1963).

John C. Schuder "Powering an Artificial Heart: Birth of the Inductively Coupled-Radio Frequency System in 1960", *Artificial Organs*, vol. 26, No. 11, pp. 909-915 (2002).

A. Mediano et al. "Design of class E amplifier with nonlinear and linear shunt capacitances for any duty cycle", IEEE Trans. Microwave Theor. Tech., vol. 55, No. 3, pp. 484-492, (2007).

H. Sekiya et al. "FM/PWM control scheme in class DE inverter", IEEE Trans. Circuits Syst. I, vol. 51, No. 7 (Jul. 2004).

Abe et al. "A Noncontact Charger Using a Resonant Converter with Parallel Capacitor of the Secondary Coil". IEEE, 36(2):444-451, Mar./Apr. 2000.

Altchev et al. "Efficient Resonant Inductive Coupling Energy Transfer Using New Magnetic and Design Criteria". IEEE, pp. 1293-1298, 2005.

T. Aoki et al. Observation of strong coupling between one atom and a monolithic microresonator. Nature 443:671-674 (2006).

Apneseth et al. "Introducing wireless proximity switches" ABB Review Apr. 2002.

Baker et al., "Feedback Analysis and Design of RF Power Links for Low-Power Bionic Systems," IEEE Transactions on Biomedical Circuits and Systems, 1(1):28-38 (Mar. 2007).

Balanis, C.A., "Antenna Theory: Analysis and Design," 3rd Edition, Sections 4.2, 4.3, 5.2, 5.3 (Wiley, New Jersey, 2005).

Burri et al. "Invention Description" Feb. 5, 2008.

Electricity Unplugged, Feature: Wireless Energy, *Physics World*, pp. 23-25 (Feb. 2009).

Esser et al. "A New Approach to Power Supplies for Robots". IEEE, 27(5):872-875, Sep./Oct. 1991.

Fenske et al. "Dielectric Materials at Microwave Frequencies". Applied Microwave & Wireless, pp. 92-100, 2000.

C. Fernandez et al., "A simple dc-dc converter for the power supply of a cochlear implant", *IEEE*, pp. 1965-1970 (2003).

D.H.Freedman. "Power on a Chip". MIT Technology Review, Nov. 2004

Geyi, Wen. A Method for the Evaluation of Small Antenna Q. IEEE Transactions on Antennas and Propagation, vol. 51, No. 8, Aug. 2003. Haus, H.A., "Waves and Fields in Optoelectronics," Chapter 7 "Coupling of Modes—Reasonators and Couplers" (Prentice-Hall, New Jersey, 1984).

Heikkinen et al. "Performance and Efficiency of Planar Rectennas for Short-Range Wireless Power Transfer at 2.45 GHz". Microwave and Optical Technology Letters, 31(2):86-91, Oct. 20, 2001.

Hirai et al. "Integral Motor with Driver and Wireless Transmission of Power and Information for Autonomous Subspindle Drive". IEEE, 15(1):13-20, Jan. 2000.

Hirai et al. "Practical Study on Wireless Transmission of Power and Information for Autonomous Decentralized Manufacturing System". IEEE, 46(2):349-359, Apr. 1999.

Hirai et al. "Study on Intelligent Battery Charging Using Inductive Transmission of Power and Information". IEEE, 15(2):335-345, Mar. 2000.

Hirai et al. "Wireless Transmission of Power and Information and Information for Cableless Linear Motor Drive". IEEE 15(1):21-27, Jan. 2000.

"Intel CTO Says Gap between Humans, Machines Will Close by 2050", *Intel News Release*, (See intel.com/.../20080821comp. htm?iid=S...) (Printed Nov. 6, 2009).

M.V. Jacob et al. "Lithium Tantalate—A High Permittivity Dielectric Material for Microwave Communication Systems". Proceedings of IEEE TENCON—Poster Papers, pp. 1362-1366, 2003.

Jackson, J.D., "Classical Electrodynamics," 3rd Edition, Sections 1.11, 5.5, 5.17, 6.9, 8.1, 8.8, 9.2, 9.3 (Wiley, New York, 1999).

Aristeidis Karalis et al., "Efficient Wireless non-radiative mid-range energy transfer", *Annals of Physics*, vol. 323, pp. 34-48 (2008).

Kawamura et al. "Wireless Transmission of Power and Information Through One High-Frequency Resonant AC Link Inverter for Robot Manipulator Applications". IEEE, 32(3):503-508, May/Jun. 1996. Yoshihiro Konishi, *Microwave Electronic Circuit Technology*, Chap-

ter 4, pp. 145-197 (Marcel Dekker, Inc., New York, NY 1998). Andre Kurs et al., "Wireless Power Transfer via Strongly Coupled Magnetic Resonances", *Science* vol. 317, pp. 83-86 (Jul. 6, 2007). Lee, "Antenna Circuit Design for RFID Applications," Microchip

Technology Inc., AN710, 50 pages (2003). Lee, "RFID Coil Design," Microchip Technology Inc., AN678, 21 pages (1998).

Liang et al., "Silicon waveguide two-photon absorption detector at 1.5 µm wavelength for autocorrelation measurements," Applied Physics Letters, 81(7):1323-1325 (Aug. 12, 2002).

Microchip Technology Inc., "microID 13.56 MHz Design Guide—MCRF355/360 Reader Reference Design," 24 pages (2001).

MIT Team Experimentally Demonstrates Wireless Power Transfer, Potentially Useful for Power Laptops, Cell-Phones Without Cords—Goodbye Wires . . . , by Franklin Hadley, Institute for Soldier Nanotechnologies, Massachusetts Institute of Technology (Jun. 7, 2007).

O'Brien et al. "Analysis of Wireless Power Supplies for Industrial Automation Systems". IEEE, pp. 367-372, 2003.

O'Brien et al. "Design of Large Air-Gap Transformers for Wireless Power Supplies". IEEE, pp. 1557-1562, 2003.

J. B. Pendry. "A Chiral Route to Negative Refraction". Science 306:1353-1355 (2004).

Gary Peterson, "MIT WiTricity Not So Original After All", Feed Line No. 9, (See http://www.tfcbooks.com/articles/witricity.htm) printed Nov. 12, 2009.

"Physics Update, Unwired Energy", *Physics Today*, pp. 26, (Jan. 2007) (See http://arxiv.org/abs/physics/0611063.).

Powercast LLC. "White Paper" Powercast simply wire free, 2003. Sakamoto et al. "A Novel Circuit for Non-Contact Charging Through Electro-Magnetic Coupling". IEEE, pp. 168-174, 1992.

Sekitani et al. "A large-area flexible wireless power transmission sheet using printed plastic MEMS switches and organic field-effect transistors". [Publication Unknown].

Sekitani et al. "A large-area wireless power-transmission sheet using printed organic transistors and plastic MEMS switches" www.nature.com/naturematerials. Published online Apr. 29, 2007.

S. Sensiper. Electromagnetic wave propogation on helical conductors. PhD Thesis, Massachusetts Institute of Technology, 1951.

Soljacic. "Wireless Non-Radiative Energy Transfer—PowerPoint presentation". Massachusetts Institute of Technology, Oct. 6, 2005. Someya, Takao. "The world's first sheet-type wireless power transmission system". University of Tokyo, Dec. 12, 2006.

Splashpower, "Splashpower—World Leaders in Wireless Power," PowerPoint presentation, 30 pages (Sep. 3, 2007).

David H. Staelin et al., *Electromagnetic Waves*, Chapters 2, 3, 4, and 8, pp. 46-176 and 336-405 (Prentice Hall Upper Saddle River, New Jersey 1998).

Nikola Tesla, "High Frequency Oscillators for Electro-Therapeutic and Other Purposes", *The Electrical Engineer*, vol. XXVI, No. 50 (Nov. 17, 1898).

Nikola Tesla, "High Frequency Oscillators for Electro-Therapeutic and Other Purposes", *Proceedings of the IEEE*, vol. 87, No. 7, pp. 1282-1292 (Jul. 1999).

Texas Instruments, "HF Antenna Design Notes—Technical Application Report," Literature No. 11-08-26-003, 47 pages (Sep. 2003).

"The Big Story for CES 2007: The public debut of eCoupled Intelligent Wireless Power" Press Release, Fulton Innovation LLC, Las Vegas, NV, Dec. 27, 2006.

"The world's first sheet-type wireless power transmission system: Will a socket be replaced by e-wall?" Press Release, Tokyo, Japan, Dec. 12, 2006.

Thomsen et al., "Ultrahigh speed all-optical demultiplexing based on two-photon absorption in a laser diode," Electronics Letters, 34(19):1871-1872 (Sep. 17, 1998).

#### (56) References Cited

#### OTHER PUBLICATIONS

"Unwired energy questions asked, answered", *Physics Today*, pp. 16-17 (Sep. 2007).

UPM Rafsec, "Tutorial overview of inductively coupled RFID Systems," 7 pages (May 2003).

Vandevoorde et al. "Wireless energy transfer for stand-alone systems: a comparison between low and high power applicability". Sensors and Actuators, A 92:305-311, 2001.

David Vilkomerson et al., "Implantable Doppler System for Self-Monitoring Vascular Grafts", *IEEE Ultrasonics Symposium*, pp. 461-465 (2004).

"Wireless Energy Transfer Can Potentially Recharge Laptops, Cell Phones Without Cords", by Marin Soljacic of Massachusetts Institute of Technology and Davide Castelvecchi of American Institute of Physics (Nov. 14, 2006).

Clemens M. Zierhofer et al., "High-Efficiency Coupling-Insensitive Transcutaneous Power and Data Transmission Via an Inductive Link", *IEEE Transactions on Biomedical Engineering*, vol. 37, No. 7, pp. 716-722 (Jul. 1990).

Examination Report for Australia Application No. 2006269374, dated Sep. 18, 2008.

International Search Report and Written Opinion for International Application No. PCT/US2006/026480, dated Dec. 21, 2007.

International Preliminary Report on Patentability for International Application No. PCT/US2006/026480, dated Jan. 29, 2008.

International Search Report and Written Opinion for International Application No. PCT/US2007/070892, dated Mar. 3, 2008.

International Search Report and Written Opinion for International Application No. PCT/US09/43970, dated Jul. 14, 2009.

European Examination Report dated Jan. 15, 2009 in connection with Application No. 06 786 588.1-1242.

International Preliminary Report on Patentability with regard to International Application No. PCT/US2007/070892 dated Sep. 29, 2000

"Recharging, The Wireless Way—Even physicists forget to recharge their cell phones sometimes." by Angela Chang—PC Magazine, *ABC News Internet Ventures*, (2006).

"Physics Promises Wireless Power" by Jonathan Fildes, Science and Technology Reporter, *BBC News*, (Nov. 15, 2006).

"Wireless energy promise powers up" by Jonathan Fildes, Science and Technology Report, *BBC News*, (See http://news.bbc.co.uk/2/hi/technology/6725955.stm) (Jun. 7, 2007).

"The technology with impact 2007", by Jonathan Fildes, *BBC News*, (Dec. 27, 2007).

"In pictures: A year in technology", BBC News, (Dec. 28, 2007).

"Man tries wirelessly boosting batteries", by Seth Borenstein, AP Science Writer, Boston.com, (See http://www.boston.com/business/technology/articles/2006/11/15/man\_tries\_wirelessly\_b . . . ) (Nov. 15, 2006).

"The vision of an MIT physicist: Getting rid of pesky rechargers" by Gareth Cooks, Globe Staff, Boston.com, (Dec. 11, 2006).

"MIT discovery could unplug your iPod forever", by Chris Reidy, Globe staff, Boston.com, (See http://www.boston.com/business/ticker/2007/06/mit\_discovery\_c.html) (Jun. 7, 2007).

"Scientists light bulb with 'wireless electricity'", www.Chinaview.cn, (See http://news.xinhuanet.com/english/2007-06/08/content\_6215681.htm) (Jun. 2007).

"Look, Ma—No wires!—Electricity broadcast through the air may someday run your home", by Gregory M. Lamb, Staff writer, *The Christian Science Monitor*, (See http://www.csmonitor.com/2006/1116/p14s01-stct.html) (Nov. 15, 2006).

"The end of the plug? Scientists invent wireless device that beams electricity through your home", by David Derbyshire, *Daily Mail*, (See <a href="http://www.dailymail.co.uk/pages/live/articles/technology/technology/html?in\_article\_id=4...">http://www.dailymail.co.uk/pages/live/articles/technology/technology/html?in\_article\_id=4...</a>) (Jun. 7, 2007).

"Lab report: Pull the plug for a positive charge", by James Morgan, *The Herald*, Web Issue 2680 (Nov. 16, 2006).

"Recharging gadgets without cables", *Infotech Online*, Printed from infotech.indiatimes.com (Nov. 17, 2006).

"Electro-nirvana? Not so fast", by Alan Boyle, MSNBC, (Jun. 8, 2007).

"Evanescent coupling' could power gadgets wirelessly" by Celeste Biever, NewScientistsTech.com, (see http://www.newscientisttech.com/article.ns?id=dn10575&print=true) (Nov. 15, 2006).

"Wireless Energy", by Clay Risen, *The New York Times*, (Dec. 9, 2007).

"Wireless power transfer possible", *PressTV*, (See http://www.presstv.ir/detail.aspx?id=12754&sectionid=3510208) (Jun. 11, 2007).

"Outlets Are Out", by Phil Berardelli, ScienceNOW Daily News, *Science Now*, (See http://sciencenow.sciencemag.org/cgi/content/full/2006/1114/2) (Nov. 14, 2006).

"The Power of Induction—Cutting the last cord could resonate with our increasingly gadget-dependent lives", by Davide Castelvecchi, *Science News Online*, vol. 172, No. 3, (Week of Jul. 21, 2007).

"Wireless Energy Transfer May Power Devices at a Distance", ScientificAmerican.com, (Nov. 14, 2006).

"Wireless Energy Lights Bulb from Seven Feet Away—Physicists vow to cut the cord between your laptop battery and the wall socket—with just a simple loop of wire", by JR Minkel, ScientificAmerican.com, (See http://www.sciam.com/article.cfm?articleid=07511C52-E7F2-99DF-3FA6ED2D7DC9AA2...) (Jun. 7, 2007).

"Air Power—Wireless data connections are common—now scientists are working on wireless power", by Stephen Cass, Sponsored by Spectrum, (See http://spectrum.ieee.org/computing/hardware/air-power) (Nov. 2006).

"Wireless revolution could spell end of plugs", by Roger Highfield, Science Editor, Telegraph.co.uk, (See http://www.telegraph.co.uk/news/main.jhtml?xml=/news/2007/06/07/nwireless107.xml) (Jun. 7, 2007).

"Man tries wirelessly boosting batteries", by Seth Borenstein, The Associated Press, *USA Today*, (Nov. 16, 2006).

"MIT's wireless electricity for mobile phones", by Miebi Senge, *Vanguard*, (See http://www.vanguardngr.com/articles/2002/features/gsm/gsm211062007.htm) (Jun. 11, 2007).

"MIT Scientists Pave the Way For Wireless Battery Charging", by William M. Bulkeley, *The Wall Street Journal*, (See http://online.wsj.com/article/SB118123955549228045.html?mod=googlenews\_wsj) (Jun. 8, 2007).

U.S. Appl. No. 60/908,383, filed Mar. 27, 2007.

"Intel Moves to Free Gadgets of Their Recharging Cords", By John Markoff, The New York Times—nytimes.com, Aug. 21, 2008.

G. Scheible et al., "Novel Wireless Power Supply System for Wireless Communication Devices in Industrial Automation Systems", *IEEE*, (2002).

J. Schutz et al., "Load Adaptive Medium Frequency Resonant Power Supply", *IEEE*, (2002).

Marin Soljacic et al., "Photonic-crystal slow-light enhancement of nonlinear phase sensitivity", *J. Opt. Soc. Am B*, vol. 19, No. 9, pp. 2052-2059 (Sep. 2002).

Amnon Yariv et al., "Coupled-resonator optical waveguide: a proposal and analysis", *Optics Letters*, vol. 24, No. 11, pp. 711-713 (Jun. 1, 1999).

International Search Report for International Application No. PCT/ US09/58499 dated Dec. 10, 2009.

PCT International Search Report and Written Opinion for PCT/US09/59244, Dec. 7, 2009, 12 pages.

Non-Final Office Action for U.S. Appl. No. 12/648,604 dated Dec. 5,

Non-Final Office Action for U.S. Appl. No. 13/036,177 dated May 15, 2012.

Non-Final Office Action for U.S. Appl. No. 13/078,511 dated May 15, 2012.

Non-Final Office Action for U.S. Appl. No. 12/726,742 dated May 11, 2012.

Non-Final Office Action for U.S. Appl. No. 13/030,395 dated May 17, 2012.

Non-Final Office Action for U.S. Appl. No. 13/040,810 dated May

Andre Kurs et al., "Simultaneous mid-range power transfer to multiple devices", *Applied Physics Letters*, vol. 96, No. 044102 (2010).

#### (56) References Cited

#### OTHER PUBLICATIONS

David Schneider, "A Critical Look at Wireless Power", *IEEE Spectrum*, (May 2010).

Mann Soljacic, "Wireless nonradiative energy transfer", Visions of Discovery New Light on Physics, Cosmology, and Consciousness, Cambridge University Press, New York, NY pp. 530-542 (2011).

Joseph C. Stark III, "Wireless Power Transmission Utilizing a Phased Array of Tesla Coils", *Master Thesis, Massachusetts Institute of Technology* (2004).

International Search Report and Written Opinion of the International Searching Authority for International Application No. PCT/US2011/027868 dated Jul. 5, 2011.

European Search Report with regard to Application Serial No. 11184066.6 dated Mar. 20, 2013.

Klaus Finkenzeller, "RFID Handbook (2<sup>nd</sup> Edition)", The Nikkan Kogyo Shimbun, Ltd., pp. 19, 20, 38, 39, 43, 44, 62, 63, 67, 68, 87, 88, 291, 292 (Published on May 31, 2004).

Translation of Information Statement by Third Party submitted to the Japanese Patent Office for Japanese Application No. 2011-83009, translation received on May 15, 2013.

Submission of Publication to the Japanese Patent Office for Japanese Application No. 2011-256,729, translation received on May 2, 2013. Submission of Publication to the Japanese Patent Office for Japanese Application No. 2011-509,705, translation received on May 2, 2013. "Automatic Recharging, From a Distance" by Anne Eisenberg, The New York Times, (see www.nytimes.com/2012/03/11/business/built-in-wireless-chargeing-for-electronic-devices.html?\_r=0) (published on Mar. 10, 2012).

"How Wireless Charging Will Make Life Simpler (And Greener)" by David Ferris, Forbes (See forbes.com/sites/davidferris/2012/07/24/how-wireless-charging-will-make-life-simpler-and-greener/print/) (dated Jul. 24, 2012).

"Wireless charging—the future for electric cars?" by Katia Moskvitch, BBC News Technology (See www.bbc.co.uk/news/technology-14183409) (dated Jul. 21, 2011).

"Next Little Thing 2010 Electricity without wires", CNN Money (See money.cnn.com/galleries/2009/smallbusiness/0911/gallery. next\_little\_thing\_2010.smb/) (dated Nov. 30, 2009).

Non-Final Office Action with regard to U.S. Appl. No. 12/949,544 dated Sep. 5, 2012 (41 pages).

Non-Final Office Action with regard to U.S. Appl. No. 12/646,524 dated Oct. 1, 2012 (11 pages).

Non-Final Office Action with regard to U.S. Appl. No. 12/415,667 dated Oct. 5, 2012 (20 pages).

Final Office Action with regard to U.S. Appl. No. 12/639,967 dated Oct. 5, 2012 (21 pages).

Final Office Action with regard to U.S. Appl. No. 12/639,966 dated Oct. 9, 2012 (20 pages).

Non-Final Office Action with regard to U.S. Appl. No. 12/868,852 dated Oct. 10, 2012 (26 pages).

Non-Final Office Action with regard to U.S. Appl. No. 12/649,635 dated Dec. 21, 2012 (41 pages).

Non-Final Office Action with regard to U.S. Appl. No. 12/649,777 dated Dec. 24, 2012 (43 pages).

Non-Final Office Action with regard to U.S. Appl. No. 12/649,813 dated Dec. 21, 2012 (40 pages).

Non-Final Office Action with regard to U.S. Appl. No. 12/649,852 dated Dec. 21, 2012 (41 pages).

Non-Final Office Action with regard to U.S. Appl. No. 12/649,904 dated Dec. 28, 2012 (43 pages).

Chinese Office Action, Application No. 201110311000.X; mailed Dec. 6, 2013; Applicant: Massachusetts Institute of Technology; 20 pages.

Canadian Office Action, Application No. 2,682,284; mailed Nov. 25, 2013; Applicant: Massachusetts Institute of Technology; 3 pages. European Office Action, Application No. 11 184 066.6; mailed Dec. 3, 2013; Applicant: Massachusetts Institute of Technology; 5 pages.

Shanhui Fan et al., "Rate-Equation Analysis of Output Efficiency and Modulation Rate of Photomic-Crystal Light-Emitting Diodes", *IEEE Journal of Quantum Electronics*, vol. 36, No. 10, pp. 1123-1130 (Oct. 2000).

Jonathan Fildes, "Wireless Energy Promise Powers Up", BBC News, Jun. 7, 2007 (See http://news.bbc.co.uk/2/hi/6725955.stm).

Klaus Finkenzeller, RFID Handbook—Fundamentals and Applications in Contactless Smart Cards—, Nikkan Kohgyo-sya, Kanno Taihei, first version, pp. 32-37, 253 (Aug. 21, 2001).

S. L. Ho et al., "A Comparative Study Between Novel Witricity and Traditional Inductive Magnetic Coupling in Wireless Charging", *IEEE Transactions on Magnetics*, vol. 47, No. 5, pp. 1522-1525 (May 2011)

Will Stewart, "The Power to Set you Free", *Science*, vol. 317, pp. 55-56 (Jul. 6, 2007).

Final Office Action with regard to U.S. Appl. No. 12/639,958 dated Jun. 6, 2013 (18 pages).

Non-Final Office Action with regard to U.S. Appl. No. 12/949,580 dated Jun. 17, 2013 (55 pages).

Final Office Action with regard to U.S. Appl. No. 12/649,635 dated Jun. 20, 2013 (20 pages).

Final Office Action with regard to U.S. Appl. No. 12/649,813 dated Jun. 24, 2013 (17 pages).

Final Office Action with regard to U.S. Appl. No. 12/649,777 dated Jun. 26, 2013 (17 pages).

Final Office Action with regard to U.S. Appl. No. 12/649,852 dated Jun. 27, 2013 (19 pages).

Final Office Action with regard to U.S. Appl. No. 12/649,904 dated Sep. 26, 2013 (23 pages).

Australian Office Action, Application No. 2007349874; mailed Apr. 27, 2011; Applicant: Massachusetts Institute of Technology; 3 pages. Australian Office Action, Application No. 2011232776; mailed Dec. 2, 2011; Applicant: Massachusetts Institute of Technology; 2 pages. Australian Office Action, Application No. 2011232776; mailed Feb. 15, 2013; Applicant: Massachusetts Institute of Technology; 3 pages. Australian Office Action, Application No. 2006269374; mailed Sep. 18, 2008; Applicant: Massachusetts Institute of Technology; 3 pages. Australian Office Action, Application No. 2010200044; mailed May 16, 2011; Applicant: Massachusetts Institute of Technology; 2 pages. Australian Office Action, Application No. 2011203137; mailed Apr. 18, 2013; Applicant: Massachusetts Institute of Technology; 3 pages. Australian Office Action, Application No. 2009246310; mailed Jun. 13, 2013; Applicant: Massachusetts Institute of Technology; 2 pages. Canadian Office Action, Application No. 2,615,123; mailed Nov. 15, 2012; Applicant: Massachusetts Institute of Technology; 4 pages. Chinese Office Action, Application No. 200780053126.3; mailed Oct. 27, 2011; Applicant: Massachusetts Institute of Technology; 6

pages. Chinese Office Action, Application No. 200780053126.3; mailed Aug. 6, 2012; Applicant: Massachusetts Institute of Technology; 11 pages.

Chinese Office Action, Application No. 200780053126.3; mailed Dec. 19, 2012; Applicant: Massachusetts Institute of Technology; 8 pages.

Chinese Office Action, Application No. 201110311000.X; mailed Jun. 18, 2013; Applicant: Massachusetts Institute of Technology; 20 pages.

Chinese Office Action, Application No. 200680032299.2; mailed Jan. 22, 2010; Applicant: Massachusetts Institute of Technology; 5 pages.

Chinese Office Action, Application No. 200680032299.2; mailed Oct. 17, 2011; Applicant: Massachusetts Institute of Technology; 9 pages.

Chinese Office Action, Application No. 200680032299.2; mailed Jun. 4, 2012; Applicant: Massachusetts Institute of Technology; 5 pages.

Chinese Office Action, Application No. 201010214681.3; mailed Jan. 26, 2011; Applicant: Massachusetts Institute of Technology; 7

Chinese Office Action, Application No. 201010214681.3; mailed Nov. 2, 2011; Applicant: Massachusetts Institute of Technology; 7 pages.

#### (56)References Cited

#### OTHER PUBLICATIONS

Chinese Office Action, Application No. 201010214681.3; mailed Feb. 13, 2012; Applicant: Massachusetts Institute of Technology; 4 pages.

Chinese Office Action, Application No. 201010214681.3; mailed May 29, 2012; Applicant: Massachusetts Institute of Technology; 4

Chinese Office Action, Application No. 201010214681.3; mailed Oct. 10, 2012; Applicant: Massachusetts Institute of Technology; 3

Chinese Office Action, Application No. 201110185992.6; mailed Apr. 11, 2012; Applicant: Massachusetts Institute of Technology; 5 pages.

Chinese Office Action, Application No. 201110185992.6; mailed Jan. 4, 2013; Applicant: Massachusetts Institute of Technology; 10

Chinese Office Action, Application No. 200980127634.0; mailed Apr. 2, 2013; Applicant: Massachusetts Institute of Technology; 11 pages.

European Office Action, Application No. 06 786 588.1; mailed Jan. 15, 2009; Applicant: Massachusetts Institute of Technology; 5 pages. European Office Action, Application No. 06 786 588.1; mailed Apr. 24, 2013; Applicant: Massachusetts Institute of Technology; 4 pages. European Office Action, Application No. 06 786 588.1; mailed Dec. 3, 2013; Applicant: Massachusetts Institute of Technology; 6 pages. Japanese Office Action, Application No. 2010-500897; mailed May 29, 2012; Applicant: Massachusetts Institute of Technology; 7 pages. Japanese Office Action, Application No. 2011-256729; mailed May 28, 2013; Applicant: Massachusetts Institute of Technology; 7 pages. Japanese Office Action, Application No. 2011-509705; mailed Jul. 16, 2013; Applicant: Massachusetts Institute of Technology; 10

Japanese Office Action, Application No. 2008-521453; mailed Jan. 4, 2011; Applicant: Massachusetts Institute of Technology; 3 pages Japanese Office Action, Application No. 2011-083009; mailed Jul. 2, 2013; Applicant: Massachusetts Institute of Technology; 5 pages. Korean Office Action, Application No. 10-2009-7022442; mailed Oct. 18, 2012; Applicant: Massachusetts Institute of Technology; 5 pages.

Korean Office Action, Application No. 10-2009-7022442; mailed Jan. 31, 2013; Applicant: Massachusetts Institute of Technology; 6

Korean Office Action, Application No. 10-2011-7023643; mailed Oct. 23, 2012; Applicant: Massachusetts Institute of Technology; 5

Korean Office Action, Application No. 10-2011-7023643; mailed Jan. 31, 2013; Applicant: Massachusetts Institute of Technology; 3

Korean Office Action, Application No. 10-2013-7013521; mailed Aug. 8, 2013; Applicant: Massachusetts Institute of Technology; 2 pages.

Korean Office Action, Application No. 10-2008-7003376; mailed Mar. 7, 2011; Applicant: Massachusetts Institute of Technology; 3

Korean Office Action, Application No. 10-2011-7013029; mailed Aug. 9, 2011; Applicant: Massachusetts Institute of Technology; 4 pages.

Jackson, J. D., "Classical Electrodynamics", 3rd Edition, Wiley, New York,1999,pp. 201-203.

Tang, S.C et al., "Evaluation of the Shielding Effects on Printed-Circuit-Board Transformers Using Ferrite Plates and Copper Sheets", IEEE Transactions on Power Electronics, vol. 17, No. 6, Nov. 2002.,pp. 1080-1088.

Villeneuve, Pierre R. et al., "Microcavities in photonic crystals: Mode symmetry, tunability, and coupling efficiency", Physical Review B, vol. 54, No. 11, Sep. 15, 1996,pp. 7837-7842

Non-Final Office Action for U.S. Appl. No. 12/649,635 dated Feb. 27, 2014 (18 pages).

Non-Final Office Action for U.S. Appl. No. 12/649,777 dated Feb. 26, 2014 (16 pages).

Non-Final Office Action for U.S. Appl. No. 12/649,813 dated Feb. 27, 2014 (16 pages.).

Non-Final Office Action for U.S. Appl. No. 12/649,852 dated Feb.

27, 2014 (17 pages).

Ahmadian et al., "Miniature Transmitter for Implantable Micro Systems", Proceedings of the 25th Annual International Conference of the IEEE EMBS Cancun, Mexico, pp. 3028-3031, Sep. 17-21, 2003. Ziaie, Babak et al., "A Low-Power Miniature Transmitter Using A Low-Loss Silicon Platform For Biotelemetry", Proceedings—19th International Conference IEEE/EMBS, pp. 2221-2224; Oct. 30-Nov. 2, 1997 (4 pages).

<sup>\*</sup> cited by examiner

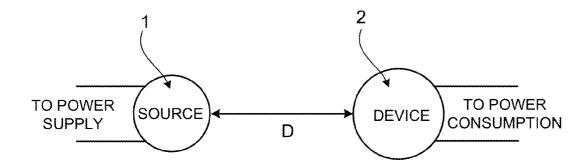


FIG. 1

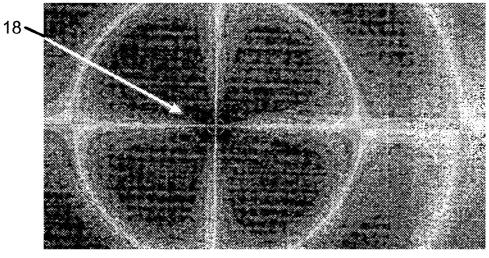


FIG. 2A

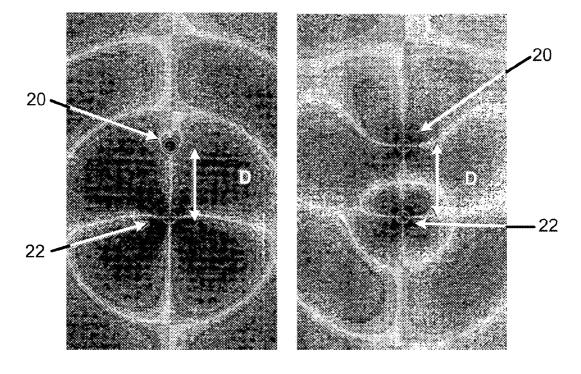


FIG. 2B

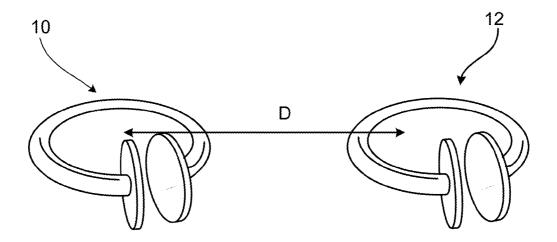
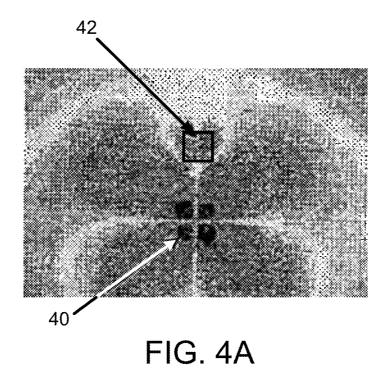


FIG. 3



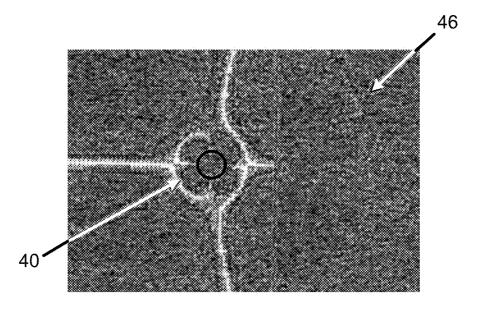


FIG. 4B

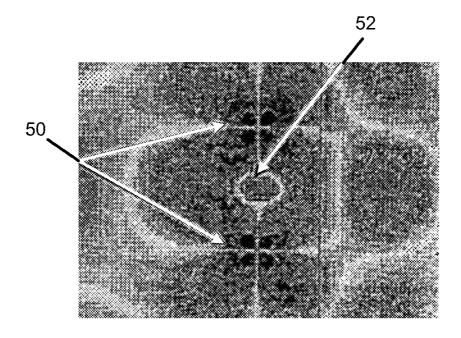
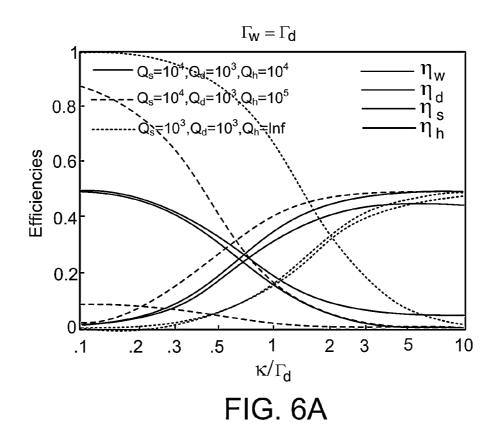
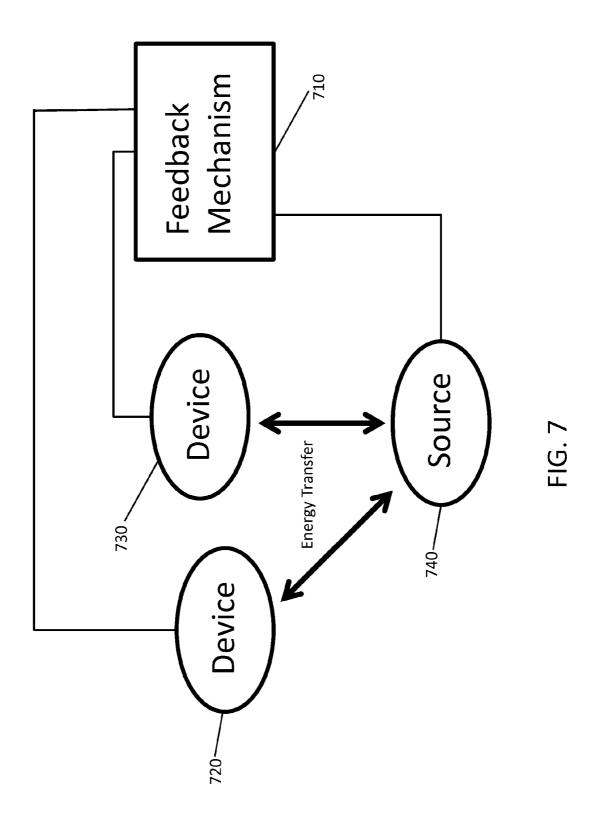


FIG. 5



 $\Gamma_{\!\!W} > \Gamma_{\!\!d}$ , optimized for each  $\kappa/\Gamma_{\!\!d}$  $Q_s=10^4, Q_d=10^3, Q_h=10^4$ 0.8 103,Qd=103,Qh=Inf Efficiencies 0.6 0.4 0.2 .3 1 2 3 5 10 .5 .1 .2  $\kappa/\Gamma_{d}$ 

FIG. 6B



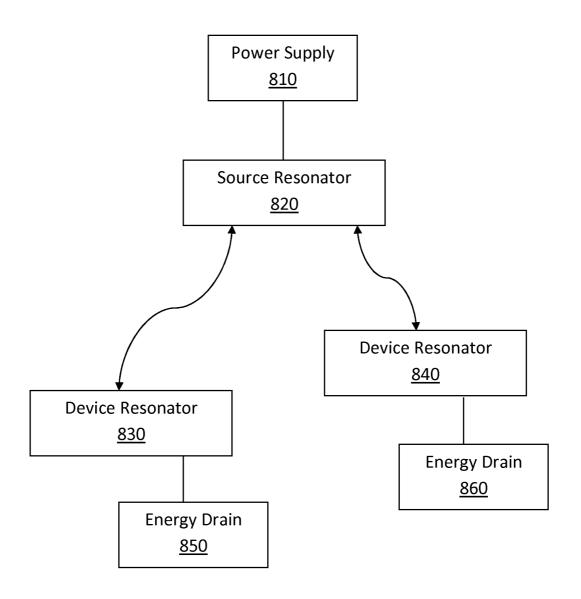


FIG. 8

# WIRELESS ENERGY TRANSFER WITH HIGH-Q TO MORE THAN ONE DEVICE

# CROSS-REFERENCE TO RELATED APPLICATIONS

This application is a continuation of U.S. patent application entitled WIRELESS NON-RADIATIVE ENERGY TRANSFER filed on Sep. 3, 2009 having Ser. No. 12/553,957 ('957 Application), the entirety of which is incorporated herein by reference. The '957 Application is a continuation of U.S. patent application entitled WIRELESS NON-RADIATIVE ENERGY TRANSFER filed on Jul. 5, 2006 and having Ser. No. 11/481,077 ('077 Application), the entirety of which is incorporated herein by reference. The '077 Application claims the benefit of provisional application Ser. No. 60/698, 442 filed Jul. 12, 2005 ('442 Application), the entirety of which is incorporated herein by reference.

This invention was made, in whole or in part by grant DMR-0213282 from the National Science Foundation. <sup>20</sup> Accordingly, the Government may have certain rights in the invention.

#### BACKGROUND OF THE INVENTION

The invention relates to the field of oscillatory resonant electromagnetic modes, and in particular to oscillatory resonant electromagnetic modes, with localized slowly evanescent field patterns, for wireless non-radiative energy transfer.

In the early days of electromagnetism, before the electrical-wire grid was deployed, serious interest and effort was devoted towards the development of schemes to transport energy over long distances wirelessly, without any carrier medium. These efforts appear to have met with little, if any, success. Radiative modes of omni-directional antennas, which work very well for information transfer, are not suitable for such energy transfer, because a vast majority of energy is wasted into free space. Directed radiation modes, using lasers or highly-directional antennas, can be efficiently used for energy transfer, even for long distances (transfer distance  $L_{TRANS} < L_{DEV}$ , where  $L_{DEV}$  is the characteristic size of the device), but require existence of an uninterruptible line-of-sight and a complicated tracking system in the case of mobile objects.

Rapid development of autonomous electronics of recent years (e.g. laptops, cell-phones, house-hold robots, that all typically rely on chemical energy storage) justifies revisiting investigation of this issue. Today, the existing electrical-wire grid carries energy almost everywhere; even a medium-range wireless non-radiative energy transfer would be quite useful. One scheme currently used for some important applications relies on induction, but it is restricted to very close-range ( $L_{TRANS} < L_{DEV}$ ) energy transfers.

#### SUMMARY OF THE INVENTION

According to one aspect of the invention, there is provided an electromagnetic energy transfer device. The electromagnetic energy transfer device includes a first resonator structure receiving energy from an external power supply. The first resonator structure has a first Q-factor. A second resonator structure is positioned distal from the first resonator structure, and supplies useful working power to an external load. The second resonator structure has a second Q-factor. The distance between the two resonators can be larger than the characteristic size of each resonator. Non-radiative energy transfer between the first resonator structure and the second

2

resonator structure is mediated through coupling of their resonant-field evanescent tails.

According to another aspect of the invention, there is provided a method of transferring electromagnetic energy. The method includes providing a first resonator structure receiving energy from an external power supply. The first resonator structure has a first Q-factor. Also, the method includes a second resonator structure being positioned distal from the first resonator structure, and supplying useful working power to an external load. The second resonator structure has a second Q-factor. The distance between the two resonators can be larger than the characteristic size of each resonator. Furthermore, the method includes transferring non-radiative energy between the first resonator structure and the second resonator structure through coupling of their resonant-field evanescent tails.

In another aspect, a method of transferring energy is disclosed including the steps of providing a first resonator structure receiving energy from an external power supply, said first resonator structure having a first resonant frequency  $\omega_1$ , and a first Q-factor  $Q_1$ , and characteristic size  $L_1$ . Providing a second resonator structure being positioned distal from said first resonator structure, at closest distance D, said second resonator structure having a second resonant frequency  $\omega_2$ , 25 and a second Q-factor  $Q_2$ , and characteristic size  $L_2$ , where the two said frequencies  $\omega_1$  and  $\omega_2$  are close to within the narrower of the two resonance widths  $\Gamma_1$ , and  $\Gamma_2$ , and transferring energy non-radiatively between said first resonator structure and said second resonator structure, said energy transfer being mediated through coupling of their resonantfield evanescent tails, and the rate of energy transfer between said first resonator and said second resonator being denoted by  $\kappa$ , where non-radiative means D is smaller than each of the resonant wavelengths  $\lambda_1$  and  $\lambda_2$ , where c is the propagation speed of radiation in the surrounding medium.

Embodiments of the method may include any of the following features. In some embodiments, said resonators have  $Q_1>100$  and  $Q_2>100$ ,  $Q_1>200$  and  $Q_2>200$ ,  $Q_1>500$  and  $Q_2>500$ , or even  $Q_1>1000$  and  $Q_2>1000$ . In some such embodiments,  $\kappa/\text{sqrt}(\Gamma_1*\Gamma_2)$  may be greater than 0.2, greater than 0.5, greater than 1, greater than 2, or even grater than 5. In some such embodiments  $D/L_2$  may be greater than 1, greater than 2, greater than 5.

In another aspect, an energy transfer device is disclosed which includes: a first resonator structure receiving energy from an external power supply, said first resonator structure having a first resonant frequency  $\omega_1$ , and a first Q-factor  $Q_1$ , and characteristic size  $L_1$ , and a second resonator structure being positioned distal from said first resonator structure, at closest distance D, said second resonator structure having a second resonant frequency  $\omega_2$ , and a second Q-factor  $Q_2$ , and characteristic size  $L_2$ .

The two said frequencies  $\omega_1$  and  $\omega_2$  are close to within the narrower of the two resonance widths  $\Gamma_1$ , and  $\Gamma_2$ . The non-radiative energy transfer between said first resonator structure and said second resonator structure is mediated through coupling of their resonant-field evanescent tails, and the rate of energy transfer between said first resonator and said second resonator is denoted by  $\kappa$ . The non-radiative means D is smaller than each of the resonant wavelengths  $\lambda_1$  and  $\lambda_2$ , where c is the propagation speed of radiation in the surrounding medium.

Embodiments of the device may include any of the following features. In some embodiments, said resonators have  $Q_1>100$  and  $Q_2>100$ ,  $Q_1>200$  and  $Q_2>200$ ,  $Q_1>500$  and  $Q_2>500$ , or even  $Q_1>1000$  and  $Q_2>1000$ . In some such embodiments,  $\kappa/\text{sqrt}(\Gamma_1*\Gamma_2)$  may be greater than 0.2, greater

than 0.5, greater than 1, greater than 2, or even grater than 5. In some such embodiments  $\mathrm{D/L_2}$  may be greater than 1, greater than 2, greater than 3, or even greater than 5.

In some embodiments, the resonant field in the device is electromagnetic.

In some embodiments, the first resonator structure includes a dielectric sphere, where the characteristic size L1 is the radius of the sphere.

In some embodiments, the first resonator structure includes a metallic sphere, where the characteristic size L1 is the  $^{10}$  radius of the sphere.

In some embodiments, the first resonator structure includes a metallodielectric sphere, where the characteristic size  $\rm L1$  is the radius of the sphere.

In some embodiments, the first resonator structure includes  $\,^{15}$  a plasmonic sphere, where the characteristic size L1 is the radius of the sphere.

In some embodiments, the first resonator structure includes a polaritonic sphere, where the characteristic size L1 is the radius of the sphere.

In some embodiments, the first resonator structure includes a capacitively-loaded conducting-wire loop, where the characteristic size L1 is the radius of the loop.

In some embodiments, the second resonator structure includes a dielectric sphere, where the characteristic size L2 <sup>25</sup> is the radius of the sphere.

In some embodiments, the second resonator structure includes a metallic sphere where the characteristic size  $L\mathbf{2}$  is the radius of the sphere.

In some embodiments, the second resonator structure <sup>30</sup> includes a metallodielectric sphere where the characteristic size L2 is the radius of the sphere.

In some embodiments, the second resonator structure includes a plasmonic sphere where the characteristic size L2 is the radius of the sphere.

In some embodiments, the second resonator structure includes a polaritonic sphere where the characteristic size L2 is the radius of the sphere.

In some embodiments, the second resonator structure includes a capacitively-loaded conducting-wire loop where 40 the characteristic size L2 is the radius of the loop.

In some embodiments, the resonant field in the device is acoustic.

It is to be understood that embodiments of the above described methods and devices may include any of the above 45 listed features, alone or in combination.

#### BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 is a schematic diagram illustrating an exemplary 50 embodiment of the invention;

FIG. 2A is a numerical FDTD result for a high-index disk cavity of radius r along with the electric field; FIG. 2B a numerical FDTD result for a medium-distance coupling between two resonant disk cavities: initially, all the energy is 55 in one cavity (left panel); after some time both cavities are equally excited (right panel).

FIG. 3 is schematic diagram demonstrating two capacitively-loaded conducting-wire loops;

FIGS. 4A-4B are numerical FDTD results for reduction in 60 radiation-Q of the resonant disk cavity due to scattering from extraneous objects;

FIG. **5** is a numerical FDTD result for medium-distance coupling between two resonant disk cavities in the presence of extraneous objects; and

FIGS. 6A-6B are graphs demonstrating efficiencies of converting the supplied power into useful work ( $\eta$ w), radiation

4

and ohmic loss at the device  $(\eta d)$ , and the source $(\eta s)$ , and dissipation inside a human  $(\eta h)$ , as a function of the coupling-to-loss ratio  $\kappa/\Gamma d$ ; in panel (a)  $\Gamma w$  is chosen so as to minimize the energy stored in the device, while in panel (b)  $\Gamma w$  is chosen so as to maximize the efficiency  $\eta w$  for each  $\kappa/\Gamma d$ .

FIG. 7 is a schematic diagram of a feedback mechanism to correct the resonators exchanging wireless energy for detuning because of the effect of an extraneous object.

FIG. 8 is a schematic diagram of an exemplary system in which a high-Q source resonator 810 is receiving power from a power supply 820 and wirelessly transfers non-radiative electromagnetic energy to multiple high-Q device resonators 830 and 840, each of which is coupled to an energy drain 850 and 860, respectively.

#### DETAILED DESCRIPTION OF THE INVENTION

In contrast to the currently existing schemes, the invention provides the feasibility of using long-lived oscillatory resonant electromagnetic modes, with localized slowly evanescent field patterns, for wireless non-radiative energy transfer. The basis of this technique is that two same-frequency resonant objects tend to couple, while interacting weakly with other off-resonant environmental objects. The purpose of the invention is to quantify this mechanism using specific examples, namely quantitatively address the following questions: up to which distances can such a scheme be efficient and how sensitive is it to external perturbations. Detailed theoretical and numerical analysis show that a mid-range (LTRANS≈few\*LDEV) wireless energy-exchange can actually be achieved, while suffering only modest transfer and dissipation of energy into other off-resonant objects.

The omnidirectional by stationary (non-lossy) nature of the near field makes this mechanism suitable for mobile wireless receivers. It could therefore have a variety of possible applications including for example, placing a source connected to a wired electricity network on the ceiling of a factory room, while devices, such as robots, vehicles, computers, or similar are roaming freely within the room. Other possible applications include electric-engine buses, RFIDs, and perhaps even nano-robots. Similarly, in some embodiments multiple sources can transfer energy to one or more device objects. For example, as explained at in the paragraph bridging pages 4-5 of U.S. Provisional Application No. 60/698,442 to which the present application claims benefit and which is incorporated by reference above, for certain applications having uneven power transfer to the device object as the distance between the device and the source changes, multiple sources can be strategically placed to alleviate the problem, and/or the peak amplitude of the source can be dynamically adjusted.

The range and rate of the inventive wireless energy-transfer scheme are the first subjects of examination, without considering yet energy drainage from the system for use into work. An appropriate analytical framework for modeling the exchange of energy between resonant objects is a weak-coupling approach called "coupled-mode theory". FIG. 1 is a schematic diagram illustrating a general description of the invention. The invention uses a source and device to perform energy transferring. Both the source 1 and device 2 are resonator structures, and are separated a distance D from each other. In this arrangement, the electromagnetic field of the system of source 1 and device 2 is approximated by  $F(r,t)\approx a1(t)F1(r)+a2(t)F2(r)$ , where F1,2(r)=[E1,2(r)H1,2(r)] are the eigenmodes of source 1 and device 2 alone, and then the field

amplitudes a1(t) and a2(t) can be shown to satisfy the "coupled-mode theory":

$$\begin{split} \frac{d\,a_1}{d\,t} &= -i(\omega_1 - i\Gamma_1)a_1 + i\kappa_{11}a_1 + i\kappa_{12}a_2 \\ \frac{d\,a_2}{d\,t} &= -i(\omega_2 - i\Gamma_2)a_2 + i\kappa_{22}a_2 + i\kappa_{21}a_1, \end{split} \tag{1}$$

where  $\omega_{1,2}$  are the individual eigen-frequencies,  $\Gamma_{1,2}$  are the resonance widths due to the objects' intrinsic (absorption, radiation etc.) losses,  $\kappa_{12,21}$  are the coupling coefficients, and  $\kappa_{11,22}$  model the shift in the complex frequency of each object due to the presence of the other.

The approach of Eq. 1 has been shown, on numerous occasions, to provide an excellent description of resonant phenomena for objects of similar complex eigen-frequencies (namely  $|\omega_1 - \omega_2| \le |\kappa_{12,21}|$  and  $\Gamma_{19} \approx \Gamma_2$ ), whose resonances are reasonably well defined (namely  $\Gamma_{1,2}$ &Im $\{\kappa_{11,22}\}$ <<  $|\kappa_{12,21}|$ ) and in the weak coupling limit (namely  $|\kappa_{12,21}|$  $\omega_{1,2}$ ). Coincidentally, these requirements also enable optimal operation for energy transfer. Also, Eq. (1) show that the energy exchange can be nearly perfect at exact resonance  $(\omega_1 = \omega_2 \text{ and } \Gamma_1 = \Gamma_2)$ , and that the losses are minimal when the "coupling-time" is much shorter than all "loss-times". Therefore, the invention requires resonant modes of high  $Q=\omega/(2\Gamma)$ for low intrinsic-loss rates  $\Gamma_{1,2}$ , and with evanescent tails significantly longer than the characteristic sizes L<sub>1</sub> and L<sub>2</sub> of the two objects for strong coupling rate  $|\kappa_{12,21}|$  over large distances D, where D is the closest distance between the two objects. This is a regime of operation that has not been studied extensively, since one usually prefers short tails, to minimize interference with nearby devices.

Objects of nearly infinite extent, such as dielectric waveguides, can support guided modes whose evanescent tails are decaying exponentially in the direction away from the object, slowly if tuned close to cutoff, and can have nearly infinite Q. To implement the inventive energy-transfer scheme, such geometries might be suitable for certain applications, but usually finite objects, namely ones that are topologically surrounded everywhere by air, are more appropriate.

Unfortunately, objects of finite extent cannot support electromagnetic states that are exponentially decaying in all directions in air, since in free space:  $\vec{k}^2 = \omega^2/c^2$ . Because of this, one can show that they cannot support states of infinite Q. However, very long-lived (so-called "high-Q") states can be found, whose tails display the needed exponential-like decay away from the resonant object over long enough distances 50 before they turn oscillatory (radiative). The limiting surface, where this change in the field behavior happens, is called the "radiation caustic", and, for the wireless energy-transfer scheme to be based on the near field rather than the far/ be such that one lies within the radiation caustic of the other.

The invention is very general and any type of resonant structure satisfying the above requirements can be used for its implementation. As examples and for definiteness, one can choose to work with two well-known, but quite different 60 electromagnetic resonant systems: dielectric disks and capacitively-loaded conducting-wire loops. Even without optimization, and despite their simplicity,  $\bar{b} oth \ will \ be \ shown$ to exhibit fairly good performance. Their difference lies mostly in the frequency range of applicability due to practical considerations, for example, in the optical regime dielectrics prevail, since conductive materials are highly lossy.

6

Consider a 2D dielectric disk cavity of radius r and permittivity ∈ surrounded by air that supports high-Q whisperinggallery modes, as shown in FIG. 2A. Such a cavity is studied using both analytical modeling, such as separation of variables in cylindrical coordinates and application of boundary conditions, and detailed numerical finite-difference-time-domain (FDTD) simulations with a resolution of 30 pts/r. Note that the physics of the 3D case should not be significantly different, while the analytical complexity and numerical requirements would be immensely increased. The results of the two methods for the complex eigen-frequencies and the field patterns of the so-called "leaky" eigenmodes are in an excellent agreement with each other for a variety of geometries and parameters of interest.

The radial modal decay length, which determines the coupling strength  $\kappa = |\kappa_{21}| = |\kappa_{12}|$ , is on the order of the wavelength, therefore, for near-field coupling to take place between cavities whose distance is much larger than their size, one needs subwavelength-sized resonant objects  $(m < \lambda)$ . High-radiation-O and long-tailed subwavelength resonances can be achieved, when the dielectric permittivity  $\in$  is as large as practically possible and the azimuthal field variations (of principal number m) are slow (namely m is small).

One such TE-polarized dielectric-cavity mode, which has the favorable characteristics  $Q_{rad}=1992$  and  $\lambda r=20$  using  $\in$ =147.7 and m=2, is shown in FIG. 2A, and will be the "test" cavity 18 for all subsequent calculations for this class of resonant objects. Another example of a suitable cavity has  $Q_{rad}$ =9100 and  $\lambda$ /r=10 using  $\in$ =65.61 and m=3. These values of s might at first seem unrealistically large. However, not only are there in the microwave regime (appropriate for meter-range coupling applications) many materials that have both reasonably high enough dielectric constants and low losses, for example, Titania:  $\in \approx 96$ , Im $\{\in\}/\in \approx 10^{-3}$ ; Barium tetratitanate:  $\in \approx 37$ , Im $\{\in\}/\in \approx 10^{-4}$ ; Lithium tantalite:  $\in \approx 40$ ,  $Im\{\in\}/\in\approx 10^{-4}$ ; etc.), but also  $\in$  could instead signify the effective index of other known subwavelength ( $\lambda/r << 1$ ) surface-wave systems, such as surface-plasmon modes on surfaces of metal-like (negative-€) materials or metallodielectric photonic crystals.

With regards to material absorption, typical loss tangents in the microwave (e.g. those listed for the materials above) suggest that  $Q_{abs} \sim \in /Im \{\in\} \sim 10000$ . Combining the effects of radiation and absorption, the above analysis implies that for a properly designed resonant device-object d a value of Q~2000 should be achievable. Note though, that the resonant source s will in practice often be immobile, and the restrictions on its allowed geometry and size will typically be much less stringent than the restrictions on the design of the device; therefore, it is reasonable to assume that the radiative losses can be designed to be negligible allowing for  $Q_s \sim 10000$ , limited only by absorption.

To calculate now the achievable rate of energy transfer, one radiation field, the distance between the coupled objects must 55 can place two of the cavities 20, 22 at distance D between their centers, as shown in FIG. 2B. The normal modes of the combined system are then an even and an odd superposition of the initial modes and their frequencies are split by the coupling coefficient κ, which we want to calculate. Analytically, coupled-mode theory gives for dielectric objects  $\kappa_{12} = \omega_2 / 2 \int d^3 r E_1 *(r) E_2(r) \in (r) / \int d^3 r |E_1(r)|^2 = (r),$  $\in_{1,2}(r)$  denote the dielectric functions of only object 1 alone or 2 alone excluding the background dielectric (free space) and  $\in$ (r) the dielectric function of the entire space with both objects present. Numerically, one can find κ using FDTD simulations either by exciting one of the cavities and calculating the energy-transfer time to the other or by determining

and a r=30 cm (household robot on the floor) loop at a distance D=3 m (room height) apart, for which  $\kappa/\sqrt{\Gamma_1\Gamma_2}$ =0.88 neaks at f=6.4 MHz, in between the peaks of the individual

peaks at f=6.4 MHz, in between the peaks of the individual Q's. Again, these values are not in the optimal regime  $\kappa/\Gamma$ <<1, but will be shown to be sufficient.

8

the split normal-mode frequencies. For the "test" disk cavity the radius  $r_C$  of the radiation caustic is  $r_C \approx 11r$ , and for nonradiative coupling D<rc, therefore here one can choose D/r=10, 7, 5, 3. Then, for the mode of FIG. 3, which is odd with respect to the line that connects the two cavities, the analytical predictions are  $\omega/2\kappa=1602,771,298,48$ , while the numerical predictions are ω/2κ=1717, 770, 298, 47 respectively, so the two methods agree well. The radiation fields of the two initial cavity modes interfere constructively or destructively depending on their relative phases and amplitudes, leading to increased or decreased net radiation loss respectively, therefore for any cavity distance the even and odd normal modes have Qs that are one larger and one smaller than the initial single-cavity Q=1992 (a phenomenon not captured by coupled-mode theory), but in a way that the average  $\Gamma$  is always approximately  $\Gamma \approx \omega/2Q$ . Therefore, the corresponding coupling-to-loss ratios are  $\kappa/\Gamma=1.16$ , 2.59, 6.68, 42.49, and although they do not fall in the ideal operating regime  $\kappa/\Gamma>>1$ , the achieved values are still large enough  $_{20}$ to be useful for applications.

Consider a loop 10 or 12 of N coils of radius r of conducting wire with circular cross-section of radius a surrounded by air, as shown in FIG. 3. This wire has inductance  $L=\mu_{\mathcal{O}}N^2r[\ln(8r/a)-2]$ , where  $\mu_{\mathcal{O}}$  is the magnetic permeability of free space, so connecting it to a capacitance C will make the loop resonant at frequency  $\omega=1/\sqrt{LC}$ . The nature of the resonance lies in the periodic exchange of energy from the electric field inside the capacitor due to the voltage across it to the magnetic field in free space due to the current in the wire. Losses in this resonant system consist of ohmic loss inside the wire and radiative loss into free space.

For non-radiative coupling one should use the near-field region, whose extent is set roughly by the wavelength  $\lambda$ , therefore the preferable operating regime is that where the loop is small (r<< $\lambda$ ). In this limit, the resistances associated with the two loss channels are respectively  $R_{ohm} = \sqrt{\mu_O \rho_0 \Omega^2} \cdot Nr/a$  and  $R_{rad} = \pi/6 \cdot \eta_O N^2 (\omega r/c)^4$ , where  $\rho$  is the resistivity of the wire material and  $\eta_O \approx 120\pi~\Omega$  is the impedance of free space. The quality factor of such a resonance is then  $Q = \omega L/(R_{ohm} + R_{rad})$  and is highest for some frequency determined by the system parameters: at lower frequencies it is dominated by ohmic loss and at higher frequencies by radiation.

To get a rough estimate in the microwave, one can use one coil (N=1) of copper ( $\rho$ =1.69·10<sup>-8</sup>  $\Omega$ m) wire and then for r=1 cm and a=1 mm, appropriate for example for a cell phone, the quality factor peaks to Q=1225 at f=380 MHz, for r=30 cm and a=2 mm for a laptop or a household robot Q=1103 at f=17 MHz, while for r=1 m and a=4 mm (that could be a source loop on a room ceiling) Q=1315 at f=5 MHz. So in general, expected quality factors are Q≈1000-1500 at  $\lambda$ /r≈50-80, namely suitable for near-field coupling.

The rate for energy transfer between two loops 10 and 12 at distance D between their centers, as shown in FIG. 3, is given by  $\kappa_{12}=\omega M/2\sqrt{L_1L_2}$ , where M is the mutual inductance of the two loops 10 and 12. In the limit  $r<<D<\lambda$  one can use the quasi-static result  $M=\pi/4\cdot\mu_ON_1N_2(r_1r_2)^2/D^3$ , which means that  $\omega/2\kappa\sim(D/\sqrt{r_1r_2})^3$ . For example, by choosing again D/r=10, 8, 6 one can get for two loops of r=1 cm, same as used 60 before, that  $\omega/2\kappa=3033$ , 1553, 655 respectively, for the r=30 cm that  $\omega/2\kappa=7131$ , 3651, 1540, and for the r=1 m that  $\omega/2\kappa=6481$ , 3318, 1400. The corresponding coupling-to-loss ratios peak at the frequency where peaks the single-loop Q and are  $\kappa/F=0.4, 0.79, 1.97$  and 0.15, 0.3, 0.72 and 0.2, 0.4, 65 0.94 for the three loop-kinds and distances. An example of dissimilar loops is that of a r=1 m (source on the ceiling) loop

It is important to appreciate the difference between this inductive scheme and the already used close-range inductive schemes for energy transfer in that those schemes are non-resonant. Using coupled-mode theory it is easy to show that, keeping the geometry and the energy stored at the source fixed, the presently proposed resonant-coupling inductive mechanism allows for Q approximately 1000 times more power delivered for work at the device than the traditional non-resonant mechanism, and this is why mid-range energy transfer is now possible. Capacitively-loaded conductive loops are actually being widely used as resonant antennas (for example in cell phones), but those operate in the far-field regime with  $r/\lambda \sim 1$ , and the radiation Q's are intentionally designed to be small to make the antenna efficient, so they are not appropriate for energy transfer.

Clearly, the success of the inventive resonance-based wireless energy-transfer scheme depends strongly on the robustness of the objects' resonances. Therefore, their sensitivity to the near presence of random non-resonant extraneous objects is another aspect of the proposed scheme that requires analysis. The interaction of an extraneous object with a resonant object can be obtained by a modification of the coupled-mode-theory model in Eq. (1), since the extraneous object either does not have a well-defined resonance or is far-off-resonance, the energy exchange between the resonant and extraneous objects is minimal, so the term  $\kappa_{12}$  in Eq. (1) can be dropped. The appropriate analytical model for the field amplitude in the resonant object  $a_1(t)$  becomes:

$$\frac{da_1}{dt} = -i(\omega_1 - i\Gamma_1)a_1 + i\kappa_{11}a_1 \tag{2}$$

Namely, the effect of the extraneous object is just a perturbation on the resonance of the resonant object and it is twofold: First, it shifts its resonant frequency through the real part of  $\kappa_{11}$  thus detuning it from other resonant objects. As shown in FIG. 7, this is a problem that can be fixed rather easily by applying a feedback mechanism 710 to every device (e.g., device resonators 720 and 730) that corrects its frequency. such as through small changes in geometry, and matches it to that of the source resonator 740. Second, it forces the resonant object to lose modal energy due to scattering into radiation from the extraneous object through the induced polarization or currents in it, and due to material absorption in the extraneous object through the imaginary part of  $\kappa_{11}$ . This reduction in Q can be a detrimental effect to the functionality of the energy-transfer scheme, because it cannot be remedied, so its magnitude must be quantified.

In the first example of resonant objects that have been considered, the class of dielectric disks, small, low-index, low-material-loss or far-away stray objects will induce small scattering and absorption. To examine realistic cases that are more dangerous for reduction in Q, one can therefore place the "test" dielectric disk cavity 40 close to: a) another off-resonance object 42, such as a human being, of large  $Re\{\in\}=49$  and  $Im\{\in\}=16$  and of same size but different shape, as shown in FIG. 4A; and b) a roughened surface 46, such as a wall, of large extent but of small  $Re\{\in\}=2.5$  and  $Im\{\in\}=0.05$ , as shown in FIG. 4B.

Analytically, for objects that interact with a small perturbation the reduced value of radiation-Q due to scattering could be estimated using the polarization  $\int d^3r |P_{X1}(r)|^2 \propto \int d^3r |E_1(r) \cdot \operatorname{Re}\{\subseteq_X(r)\}|^2$  induced by the resonant cavity 1 inside the extraneous object X=42 or roughened surface 5 X=46. Since in the examined cases either the refractive index or the size of the extraneous objects is large, these first-order perturbation-theory results would not be accurate enough, thus one can only rely on numerical FDTD simulations. The absorption-Q inside these objects can be estimated through  $\operatorname{Im}\{\kappa_{11}\}=\omega_1/2\cdot\int d^3r |E_1(r)|^2\operatorname{Im}\{\in_X(r)\}/\int d^3r |E_1(r)|^2\in(r)$ .

Using these methods, for distances D/r=10, 7, 5, 3 between the cavity and extraneous-object centers one can find that  $Q_{rad}$ =1992 is respectively reduced to  $Q_{rad}$ =1988, 1258, 702, 226, and that the absorption rate inside the object is  $Q_{abs}$ =312530, 86980, 21864, 1662, namely the resonance of the cavity is not detrimentally disturbed from high-index and/or high-loss extraneous objects, unless the (possibly mobile) object comes very close to the cavity. For distances D/r=10, 7, 5, 3, 0 of the cavity to the roughened surface we 20 find respectively Q<sub>rad</sub>=2101, 2257, 1760, 1110, 572, and  $Q_{abs}$ >4000, namely the influence on the initial resonant mode is acceptably low, even in the extreme case when the cavity is embedded on the surface. Note that a close proximity of metallic objects could also significantly scatter the resonant 25 field, but one can assume for simplicity that such objects are not present.

Imagine now a combined system where a resonant sourceobject s is used to wirelessly transfer energy to a resonant device-object d but there is an off-resonance extraneous-object e present. One can see that the strength of all extrinsic loss mechanisms from e is determined by  $|E_s(r_e)|^2$ , by the square of the small amplitude of the tails of the resonant source, evaluated at the position r<sub>e</sub> of the extraneous object. In contrast, the coefficient of resonant coupling of energy from the 35 source to the device is determined by the same-order tail amplitude  $|E_s(r_d)|$ , evaluated at the position  $r_d$  of the device, but this time it is not squared! Therefore, for equal distances of the source to the device and to the extraneous object, the coupling time for energy exchange with the device is much 40 shorter than the time needed for the losses inside the extraneous object to accumulate, especially if the amplitude of the resonant field has an exponential-like decay away from the source. One could actually optimize the performance by designing the system so that the desired coupling is achieved 45 with smaller tails at the source and longer at the device, so that interference to the source from the other objects is minimal

The above concepts can be verified in the case of dielectric disk cavities by a simulation that combines FIGS. **2A-2B** and **4A-4B**, namely that of two (source-device) "test" cavities **50** 50 placed **10**r apart, in the presence of a same-size extraneous object **52** of  $\in$  49 between them, and at a distance **5**r from a large roughened surface **56** of  $\in$  2.5, as shown in FIG. **5**. Then, the original values of Q=1992,  $\omega/2\kappa$ =1717 (and thus  $\kappa/\Gamma$ =1.16) deteriorate to Q=765,  $\omega/2\kappa$ =965 (and thus 55  $\kappa/\Gamma$ =0.79). This change is acceptably small, considering the extent of the considered external perturbation, and, since the system design has not been optimized, the final value of coupling-to-loss ratio is promising that this scheme can be useful for energy transfer.

In the second example of resonant objects being considered, the conducting-wire loops, the influence of extraneous objects on the resonances is nearly absent. The reason for this is that, in the quasi-static regime of operation ( $r << \lambda$ ) that is being considered, the near field in the air region surrounding the loop is predominantly magnetic, since the electric field is localized inside the capacitor. Therefore, extraneous objects

10

that could interact with this field and act as a perturbation to the resonance are those having significant magnetic properties (magnetic permeability  $Re\{\mu\}>1$  or magnetic loss  $Im\{\mu\}>0$ ). Since almost all common materials are non-magnetic, they respond to magnetic fields in the same way as free space, and thus will not disturb the resonance of a conducting-wire loop. The only perturbation that is expected to affect these resonances is a close proximity of large metallic structures

An extremely important implication of the above fact relates to safety considerations for human beings. Humans are also non-magnetic and can sustain strong magnetic fields without undergoing any risk. This is clearly an advantage of this class of resonant systems for many real-world applications. On the other hand, dielectric systems of high (effective) index have the advantages that their efficiencies seem to be higher, judging from the larger achieved values of  $\kappa/\Gamma$ , and that they are also applicable to much smaller length-scales, as mentioned before.

Consider now again the combined system of resonant source s and device d in the presence of a human h and a wall, and now let us study the efficiency of this resonance-based energy-transfer scheme, when energy is being drained from the device for use into operational work. One can use the parameters found before: for dielectric disks, absorptiondominated loss at the source Q<sub>s</sub>~10<sup>4</sup>, radiation-dominated loss at the device  $Q_d \sim 10^3$  (which includes scattering from the human and the wall), absorption of the source- and deviceenergy at the human  $Q_{s-h}$ ,  $Q_{d-h} \sim 10^4 - 10^5$  depending on his/her not-very-close distance from the objects, and negligible absorption loss in the wall; for conducting-wire loops,  $Q_{c} \sim Q_{c} \sim 10^{3}$ , and perturbations from the human and the wall are negligible. With corresponding loss-rates  $\Gamma = \omega/2Q$ , distance-dependent coupling  $\kappa$ , and the rate at which working power is extracted  $\Gamma_{w}$ , the coupled-mode-theory equation for the device field-amplitude is

$$\frac{da_d}{dt} = -i(\omega - i\Gamma_d)a_d + i\kappa a_s - \Gamma_{d-h}a_d - \Gamma_w a_d.$$
(3)

Different temporal schemes can be used to extract power from the device and their efficiencies exhibit different dependence on the combined system parameters. Here, one can assume steady state, such that the field amplitude inside the source is maintained constant, namely  $a_s(t) = A_s e^{-i\omega t}$ , so then the field amplitude inside the device is  $a_d(t) = A_d e^{-i\omega t}$  with  $A_d = i\kappa/(\Gamma_d + \Gamma_{d-h} + \Gamma_w)A_s$ . Therefore, the power lost at the source is  $P_s = 2\Gamma_s |A_s|^2$ , at the device it is  $P_d = 2\Gamma_d |A_d|^2$ , the power absorbed at the human is  $P_h = 2\Gamma_{s-h}|A_s|^2 + 2\Gamma_{d-h}|A_d|^2$ , and the useful extracted power is  $P_w = 2\Gamma_w|A_d|^2$ . From energy conservation, the total power entering the system is  $P_{total} = P_s + P_d + P_h + P_w$ . Denote the total loss-rates  $\Gamma_s^{tot} = \Gamma_s + \Gamma_{s-h}$  and  $\Gamma_d^{tot} = \Gamma_d + \Gamma_{d-h}$ . Depending on the targeted application, the work-drainage rate should be chosen either  $\Gamma_w = \Gamma_d^{tot}$  minimize the required energy stored in the resonant objects or  $\Gamma_w = \Gamma_d^{tot} \sqrt{1 + \kappa^2 / \Gamma_s^{tot} \Gamma_d^{tot}} > \Gamma_d^{tot}$  such that the ratio of usefulto-lost powers, namely the efficiency  $\eta_w = P_w/P_{total}$ , is maximized for some value of  $\kappa$ . The efficiencies  $\eta$  for the two different choices are shown in FIGS. 6A and 6B respectively, as a function of the  $\kappa/\Gamma_d$  figure-of-merit which in turn depends on the source-device distance.

FIGS. 6A-6B show that for the system of dielectric disks and the choice of optimized efficiency, the efficiency can be large, e.g., at least 40%. The dissipation of energy inside the human is small enough, less than 5%, for values  $\kappa/\Gamma_{e}>1$  and

 $Q_h > 10^5$ , namely for medium-range source-device distances  $(D_d/r < 10)$  and most human-source/device distances  $(D_h/r > 8)$ . For example, for  $D_d/r = 10$  and  $D_h/r = 8$ , if 10W must be delivered to the load, then, from FIG. 6B, ~0.4 W will be dissipated inside the human, ~4 W will be absorbed inside the source, and ~2.6 W will be radiated to free space. For the system of conducting-wire loops, the achieved efficiency is smaller, ~20% for  $\kappa/\Gamma_d = 1$ , but the significant advantage is that there is no dissipation of energy inside the human, as explained earlier

Even better performance should be achievable through optimization of the resonant object designs. Also, by exploiting the earlier mentioned interference effects between the radiation fields of the coupled objects, such as continuouswave operation at the frequency of the normal mode that has the larger radiation-Q, one could further improve the overall system functionality. Thus the inventive wireless energy-transfer scheme is promising for many modern applications. Although all considerations have been for a static geometry, all the results can be applied directly for the dynamic geometries of mobile objects, since the energy-transfer time  $\kappa^{-1}{\sim}1$   $\mu s$ , which is much shorter than any timescale associated with motions of macroscopic objects.

The invention provides a resonance-based scheme for mid- 25 range wireless non-radiative energy transfer. Analyses of very simple implementation geometries provide encouraging performance characteristics for the potential applicability of the proposed mechanism. For example, in the macroscopic world, this scheme could be used to deliver power to robots and/or computers in a factory room, or electric buses on a highway (source-cavity would in this case be a "pipe" running above the highway). In the microscopic world, where much smaller wavelengths would be used and smaller powers are needed, one could use it to implement optical inter-connects for CMOS electronics or else to transfer energy to autonomous nano-objects, without worrying much about the relative alignment between the sources and the devices; energy-transfer distance could be even longer compared to 40 the objects' size, since  $\operatorname{Im}\{\subseteq(\kappa)\}$  of dielectric materials can be much lower at the required optical frequencies than it is at microwave frequencies. Accordingly, FIG. 8 is a schematic drawing showing an exemplary system in which a high-Q source resonator **810** is receiving power from a power supply 45 820 and wirelessly transfers non-radiative electromagnetic energy to multiple high-Q device resonators 830 and 840, each of which is coupled to an energy drain 850 and 860,

As a venue of future scientific research, different material systems should be investigated for enhanced performance or different range of applicability. For example, it might be possible to significantly improve performance by exploring plasmonic systems. These systems can often have spatial variations of fields on their surface that are much shorter than the free-space wavelength, and it is precisely this feature that enables the required decoupling of the scales: the resonant object can be significantly smaller than the exponential-like tails of its field. Furthermore, one should also investigate using acoustic resonances for applications in which source and device are connected via a common condensed-matter object.

Although the present invention has been shown and described with respect to several preferred embodiments thereof, various changes, omissions and additions to the form 65 and detail thereof, may be made therein, without departing from the spirit and scope of the invention.

12

What is claimed is:

- 1. A system, comprising:
- a source resonator having a resonant frequency  $\omega_1$ , an intrinsic loss rate  $\Gamma_1$ , and capable of storing electromagnetic energy with a high intrinsic quality factor  $Q_1 = \omega_1/(2\Gamma_1)$ , the source resonator configured to be coupled to an energy source;
- a second resonator having a resonant frequency  $\omega_2$ , an intrinsic loss rate  $\Gamma_2$ , and capable of storing electromagnetic energy with a high intrinsic quality factor  $Q_2 = \omega_2 / (2\Gamma_2)$ , the second resonator located a distance from the source resonator; and
- a third resonator having a resonant frequency  $\omega_3$ , an intrinsic loss rate  $\Gamma_2$ , and capable of storing electromagnetic energy with a high intrinsic quality factor  $Q_3 = \omega_3/(2\Gamma_3)$ , the third resonator located a distance from the source resonator.
- wherein the source resonator and at least one of the second resonator and third resonator are configured to be coupled to wirelessly transfer electromagnetic energy from said source resonator to said at least one of the second resonator and third resonator when the source resonator is coupled to the energy source, and

wherein  $Q_1 > 100$  and  $Q_2 > 100$ ,

- wherein the resonators are movable relative to one another and wherein the wireless energy transfer occurs over a range of distances, and
- wherein  $\kappa/\sqrt{\Gamma_1\Gamma_2}>0.2$  over the range of distances, wherein  $\kappa$  is the wireless energy transfer rate.
- 2. The system of claim 1, further comprising the energy source coupled to the source resonator.
- 3. The system of claim 1, further comprising an energy drain configured to be coupled to the second resonator and an energy drain configured to be coupled to the third resonator.
- **4**. The system of claim **3**, wherein at least one of the energy drains comprises a robot, vehicle, computer, cell phone, or a portable electronic device.
- 5. The system of claim 4, wherein the at least one of the second resonator and third resonator is configured to provide useful power to the energy drain based on wirelessly transferred electromagnetic energy.
- **6**. The system of claim **1**, wherein each intrinsic loss rate comprises a resistive component and a radiative component.
- 7. The system of claim 1, wherein the source resonator is electromagnetically coupled to each of the second and third resonators.
- **8**. The system of claim **7**, wherein the source resonator is configured to wirelessly transfer electromagnetic energy from the source resonator to each of the second and third resonators.
  - 9. The system of claim 1, wherein  $Q_3 > 100$ .
- 10. The system of claim 1, wherein at least one of the resonators is tunable.
- 11. The system of claim 1, wherein the range of distances includes 5 cm.
- 12. The system of claim 1, wherein the range of distances includes 10 cm.
- 13. The system of claim 1, wherein the range of distances includes  $30\ cm$ .
- 14. The system of claim 1, wherein  $\kappa/\sqrt{\Gamma_2\Gamma_2}>0.5$  over the range of distances.
- 15. The system of claim 1, wherein  $\kappa/\sqrt{\Gamma_1\Gamma_2}>1$  over the range of distances.
- 16. The system of claim 1, wherein the efficiency of the wireless energy transfer is at least 20% over the range of distances.

- 17. The system of claim 1, wherein frequencies  $f_1=\omega_1/2\pi$ ,  $f_2=\omega_2/2\pi$ , and  $f_3=\omega_3/2\pi$  of the resonators are each at least 5 MHz
- **18**. The system of claim **1**, further comprising a feedback mechanism coupled to at least one of the resonators to correct 5 for detuning to correct for detuning of the resonant frequencies.
- 19. The system of claim 1, wherein the energy source is coupled to the source resonator, an energy drain is coupled to the second resonator, and the source resonator is electromagnetically coupled to the second resonator, and wherein the energy source and energy drain are configured to be driven to increase the ratio of useful-to-lost power for varying wireless energy transfer rates κ between the source resonator and the second resonator.
- 20. The system of claim 1, wherein the source resonator is electromagnetically coupled to the second resonator, and wherein the source resonator and second resonator are configured to be adjustably tuned to increase the ratio of useful-to-lost power for varying wireless energy transfer rates  $\kappa$  20 between the source resonator and the second resonator.
- 21. The system of claim 1, wherein the source resonator and the second resonator have different characteristic sizes.
- **22**. The system of claim **1**, wherein  $f_1=\omega_1/(2\pi)$ ,  $f_2=\omega_2/(2\pi)$ , and  $f_3=\omega_3/(2\pi)$ , and each of  $f_1$ ,  $f_2$ , and  $f_3$  is between about 5 25 MHz and 380 MHz.
  - 23. A method, comprising:

providing a source resonator having a resonant frequency  $\omega_1$ , an intrinsic loss rate  $\Gamma_1$ , and capable of storing electromagnetic energy with a high intrinsic quality factor  $_{30}$   $Q_1$  = $\omega_1$  /(2 $\Gamma_1$ ), the source resonator configured to be coupled to an energy source;

providing a second resonator having a resonant frequency  $\omega_2$ , an intrinsic loss rate  $\Gamma_2$ , and capable of storing electromagnetic energy with a high intrinsic quality factor 35  $Q_2 = \omega_2/(2\Gamma_2)$ , the second resonator located a distance from the source resonator; and

providing a third resonator having a resonant frequency  $\omega_3$ , an intrinsic loss rate  $\Gamma_3$ , and capable of storing electromagnetic energy with a high intrinsic quality factor 40  $Q_3 = \omega_3/(2\Gamma_3)$ , the third resonator located a distance from the source resonator,

wherein the source resonator and at least one of the second resonator and third resonator are configured to be coupled to wirelessly transfer electromagnetic energy 45 from said source resonator to said at least one of the second resonator and third resonator when the source resonator is coupled to the energy source,

wherein  $Q_1 > 100$  and  $Q_2 > 100$ ,

wherein the resonators are movable relative to one another 50 and wherein the wireless energy transfer occurs over a range of distances, and

wherein  $\kappa/\sqrt{\Gamma_1\Gamma_2}$ >0.2 over the range of distances, wherein  $\kappa$  is the wireless energy transfer rate.

- **24**. The method of claim **23**, wherein the source resonator  $^{55}$  and the second resonator have different characteristic sizes.
- 25. The method of claim 23, wherein the source resonator is electromagnetically coupled to the second resonator, and wherein the source resonator and second resonator are adjust-

14

ably tuned to increase the ratio of useful-to-lost power for varying wireless energy transfer rates  $\kappa$  between the source resonator and the second resonator.

- **26**. The method of claim **23**, wherein the energy source is coupled to the source resonator.
- 27. The method of claim 23, wherein an energy drain is coupled to the second resonator and an energy drain is coupled to the third resonator.
- 28. The method of claim 27, wherein at least one of the energy drains comprises a robot, vehicle, computer, cell phone, or a portable electronic device.
- 29. The method of claim 27, wherein the at least one of the second resonator and third resonator is configured to provide useful power to the energy drain based on wirelessly transferred electromagnetic energy.
- 30. The method of claim 23, wherein each intrinsic loss rate comprises a resistive component and a radiative component.
- 31. The method of claim 23, wherein the source resonator is electromagnetically coupled to each of the second and third resonators.
- 32. The method of claim 31, wherein the source resonator is configured to wirelessly transfer electromagnetic energy from the source resonator to each of the second and third resonators.
- 33. The method of claim 23, wherein  $Q_3 > 100$ .
- 34. The method of claim 23, wherein at least one of the resonators is tunable.
- 35. The method of claim 23, wherein the range of distances includes 5 cm.
- **36**. The method of claim **23**, wherein the range of distances includes 10 cm.
- 37. The method of claim 23, wherein the range of distances includes  $30 \ \text{cm}$ .
- **38**. The method of claim **23**, wherein  $\kappa/\sqrt{\Gamma_1\Gamma_2}>0.5$  over the range of distances.
- **39**. The method of claim **23**, wherein  $\kappa/\sqrt{\Gamma_1\Gamma_2}>1$  over the range of distances.
- **40**. The method of claim **23**, wherein the efficiency of the wireless energy transfer is at least 20% over the range of distances.
- **41**. The method of claim **23**, wherein frequencies  $f_1 = \omega_1/2\pi$ ,  $f_2 = \omega_2/2\pi$ , and  $f_3 = \omega_3/2\pi$  of the resonators are each at least 5 MHz.
- **42**. The method of claim **23**, wherein a feedback mechanism is coupled to at least one of the resonators to correct for detuning to correct for detuning of the resonant frequencies.
- 43. The method of claim 23, wherein the energy source is coupled to the source resonator, an energy drain is coupled to the second resonator, and the source resonator is electromagnetically coupled to the second resonator, and wherein the energy source and energy drain is driven to increase the ratio of useful-to-lost power for varying wireless energy transfer rates  $\kappa$  between the source resonator and the second resonator.
- **44**. The method of claim **23**, wherein  $f_1=\omega_1/(2\pi)$ ,  $f_2=\omega_2/(2\pi)$ , and  $f_3=\omega_3/(2\pi)$ , and each of  $f_1$ ,  $f_2$ , and  $f_3$  is between about 5 MHz and 380 MHz.

\* \* \* \* \*